

# Designing Interactive Systems I

Introduction, The CMN Model, Fitts' Law

**Prof. Dr. Jan Borchers**  
Media Computing Group  
RWTH Aachen University

Winter Semester '23/'24

<https://hci.rwth-aachen.de/dis>



**RWTH**AACHEN  
UNIVERSITY

# Who am I?



Studied CS at Karlsruhe (& Imperial)

- Human-Computer Interaction

PhD CS, TU Darmstadt (& Linz, Ulm)

- Interaction with multimedia
- HCI design patterns

Assistant professor at Stanford & ETH Zurich

- Interactive rooms
- UbiComp user interfaces

Full professor at RWTH since Oct. 2003

- Augmented Reality, Wearable & Textile UIs
- Personal Fabrication, IDEs, Soft Robotics



# Our Team



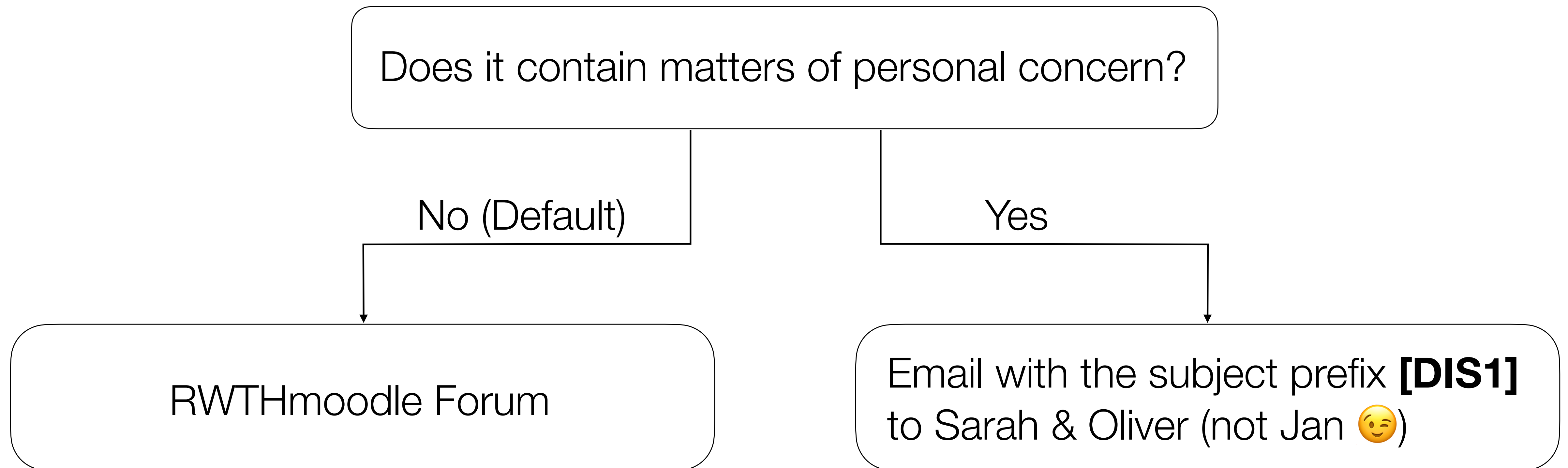
**Sarah Sahabi, M. Sc.**  
[sahabi@cs.rwth-aachen.de](mailto:sahabi@cs.rwth-aachen.de)



**Oliver Nowak, M. Sc.**  
[nowak@cs.rwth-aachen.de](mailto:nowak@cs.rwth-aachen.de)



# The Question Flow Chart :)



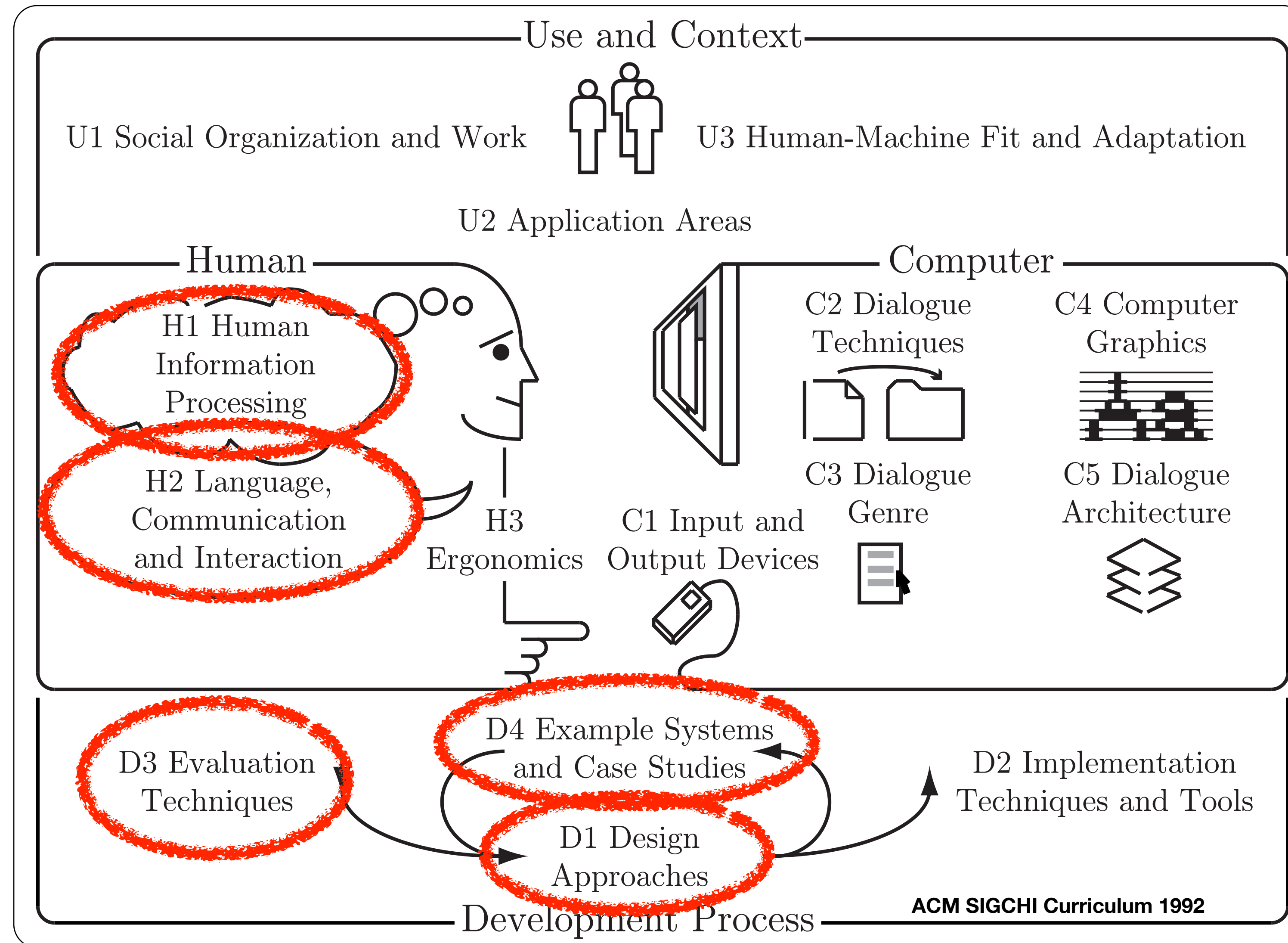
**Alternatively:** A quick chat after the lecture ☕



# Human–Computer Interaction?



# What is HCI?





# Class Topics

## Human

- Performance
- Models of interaction
  - Affordances
  - Mappings
  - Constraints
  - Types of knowledge
  - Errors
- Design principles

## Case Studies

- History of HCI
- Visions
- Phases of Technology

## Development Process

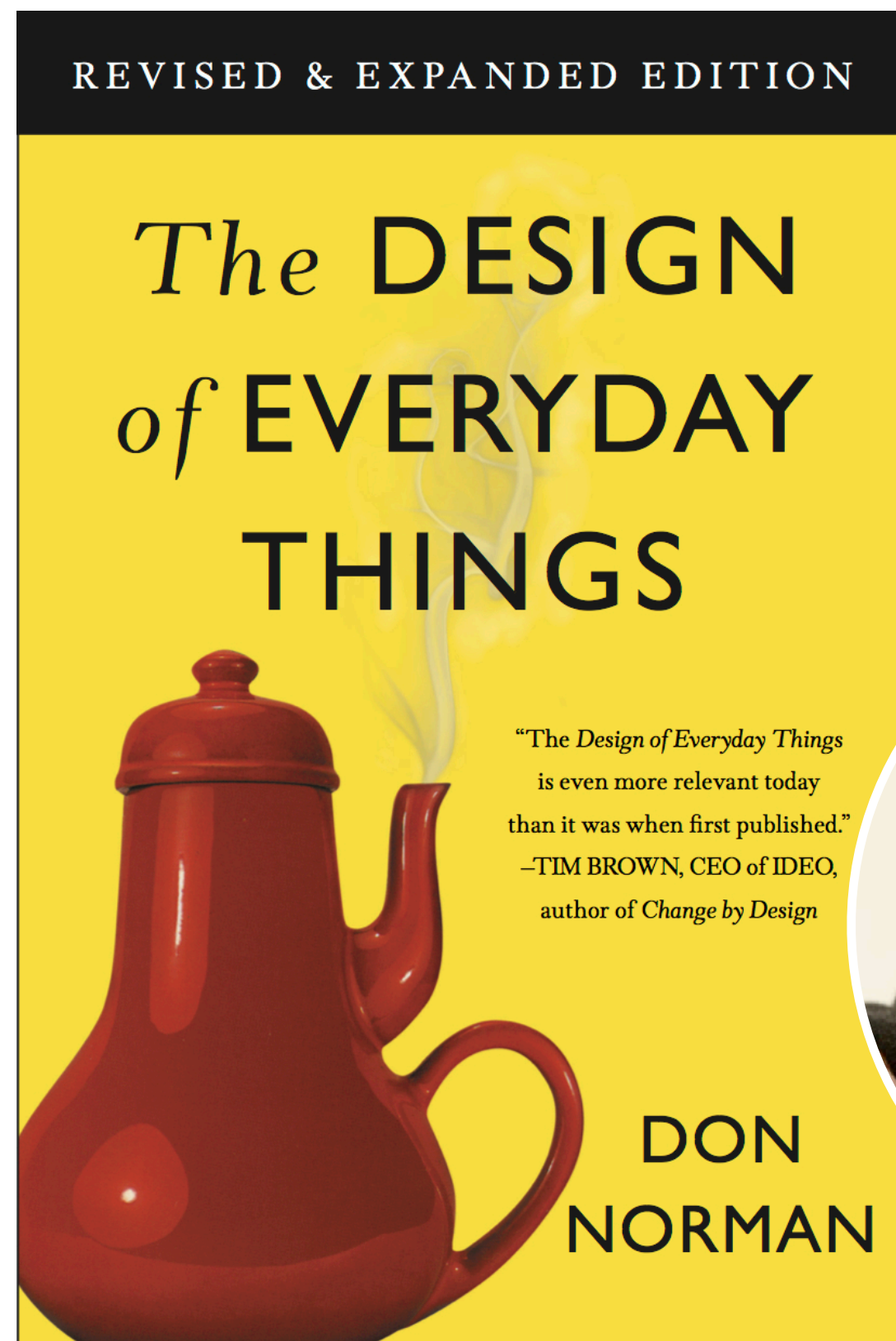
- Iterative design
- User observation
- Ideation
- Prototyping
- User studies and evaluation
- Interaction design notation

For more details, see [hci.rwth-aachen.de/dis](https://hci.rwth-aachen.de/dis).

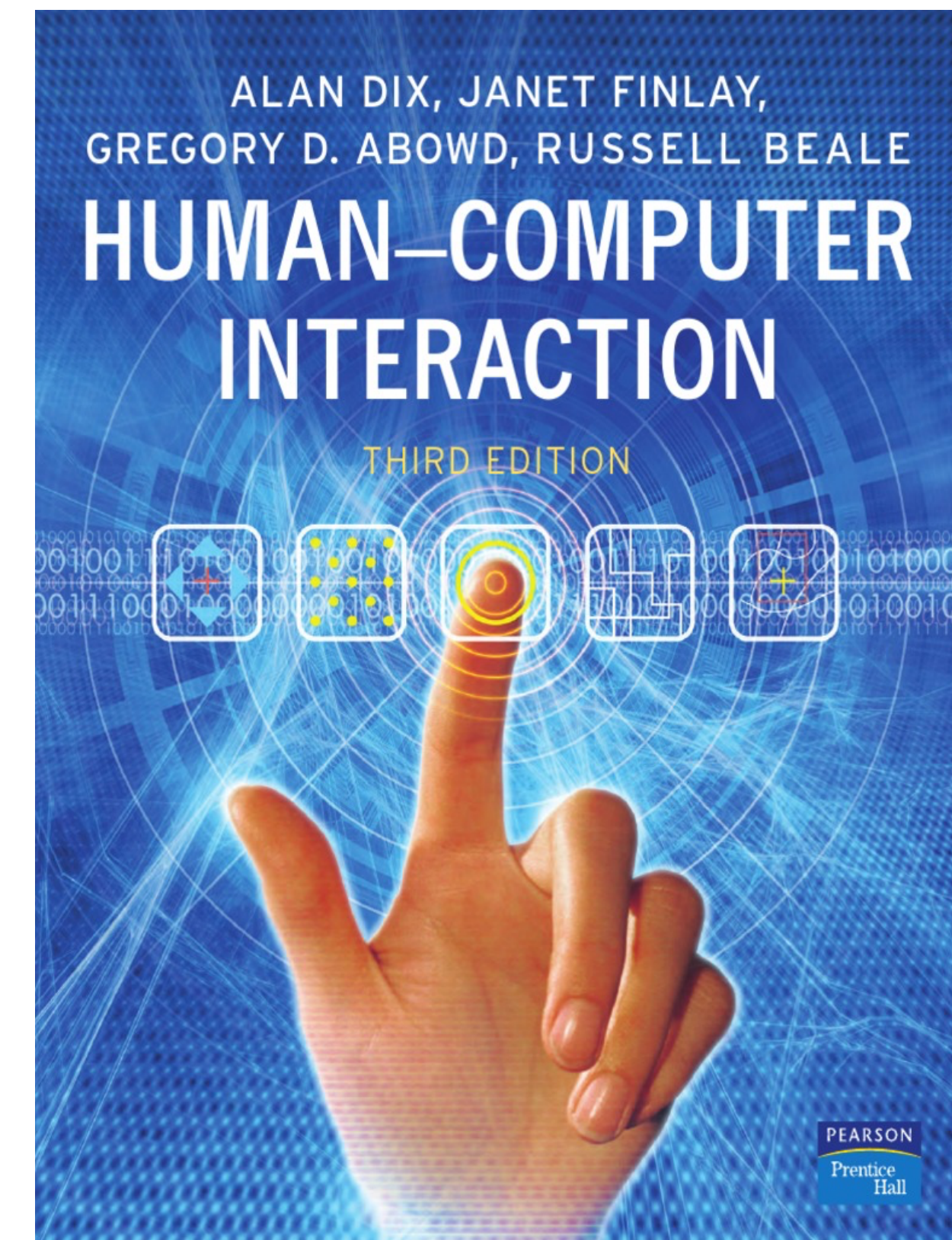


# Textbooks

## Required Reading



## Recommended Reading





# Media Computing Group



# Our Classes

When?	Type	Credits (ECTS)	Name
WS	P	7	The Media Computing Project
WS, SS	S	4	Post-Desktop User Interfaces
SS	V/Ü	6	Current Topics in HCI
WS	V/Ü	6	iOS Application Development
SS	V/Ü	6	Designing Interactive Systems II
WS	V/Ü	6	Designing Interactive Systems I
Only for B.Sc. students			
SS	PS	4	Human-Computer Interaction
SS	SW-Pr	7	M3: Multimodal Media Madness



# Course Structure



# Course Structure

## Flipped-Classroom Lecture

Watch videos at home; Discuss content in class

## Lab

- Discuss assignments

Oct 24th – Dec 5th

Midterm

## UX Project (graded)

- Create your own UX project in a group of six
- Finally, showcase your project in a video

Dec 12th – Jan 30st

Final Exam

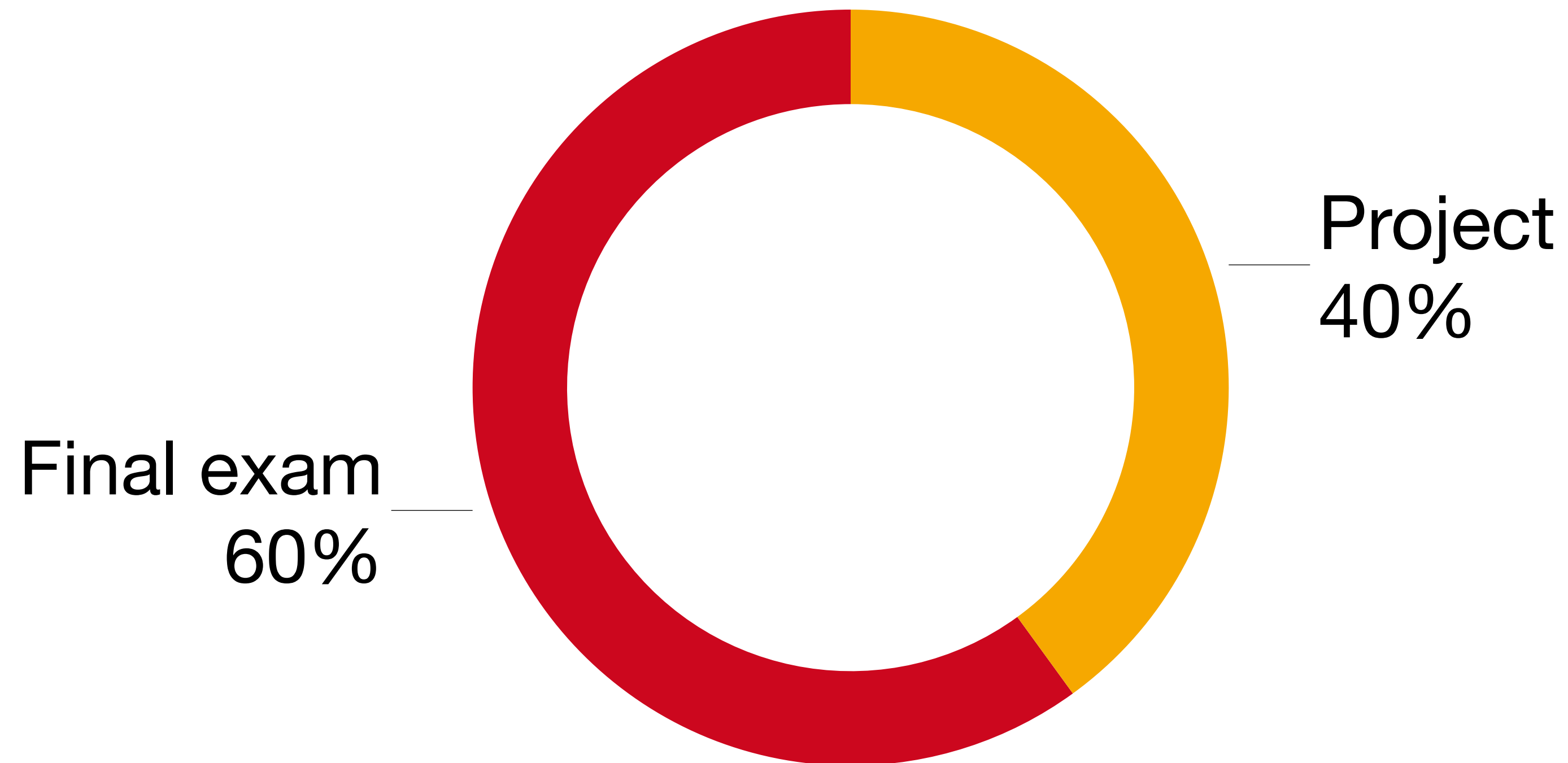
Feb  
14th

Final Exam

Mar  
12th



# Final Grade Distribution



! To pass the course, you must pass both project and final exam.

# Registering for this Class

- Register via RWTHonline and upload the **Declaration of Compliance** until **tomorrow, Oct 25, at 23:59**
  - You can also sign and submit it today
- If you want to, **you can visit the class in Aachen**, but it might happen that traveling to Bonn is necessary during the project
  - **Register for both DIS1 courses in RWTHonline**
  - **Write us an email** with the subject “**[DIS1] Moodle Access for MI**” with your name and matriculation number



# The Human



# Model Human Processor: The CMN Model

## The Psychology of Human-Computer Interaction

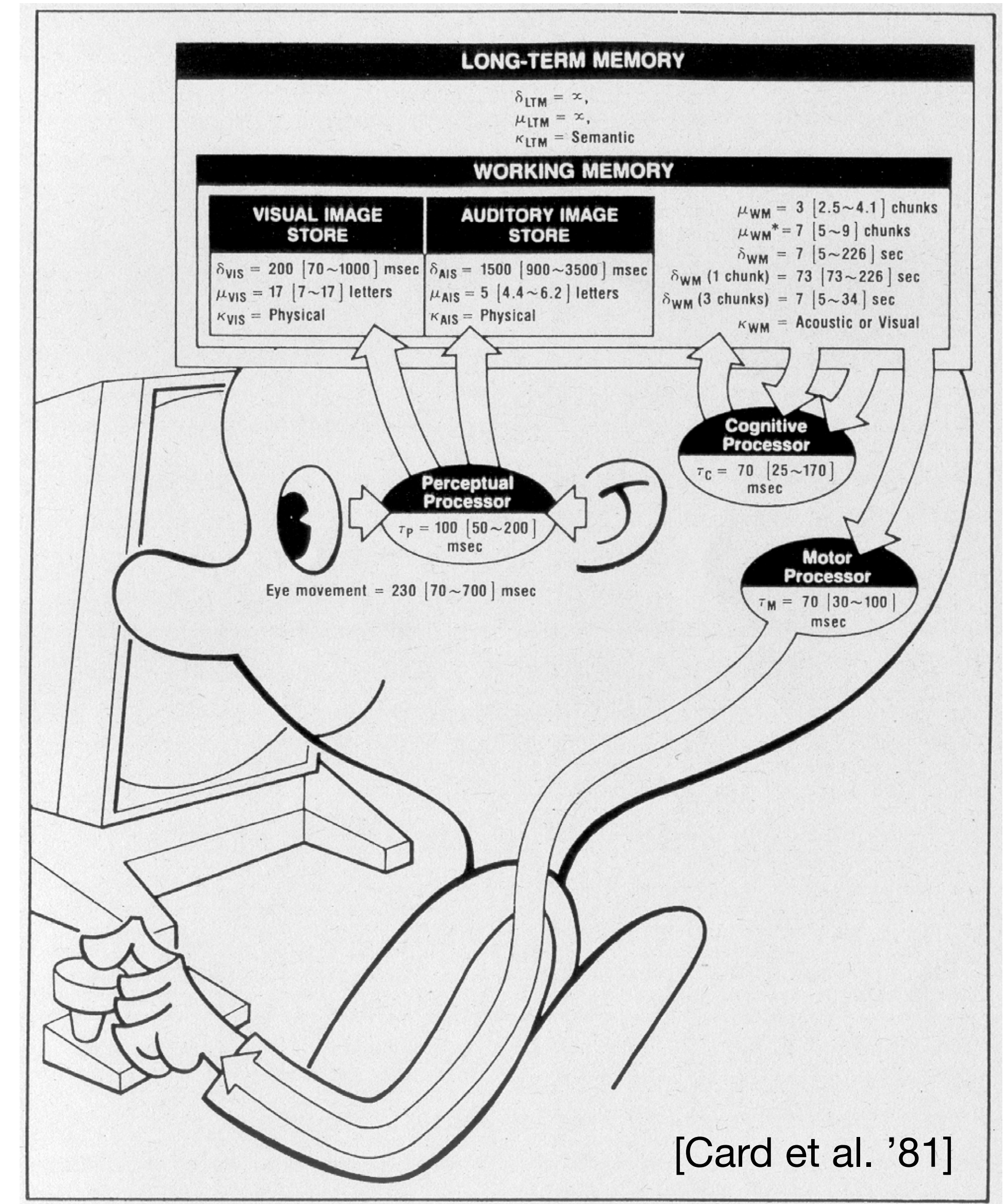
STUART K. CARD  
THOMAS P. MORAN  
ALLEN NEWELL

 CRC Press  
Taylor & Francis Group



# Model Human Processor

- 3 processors with associated memory
- Slow, middle, fast performers





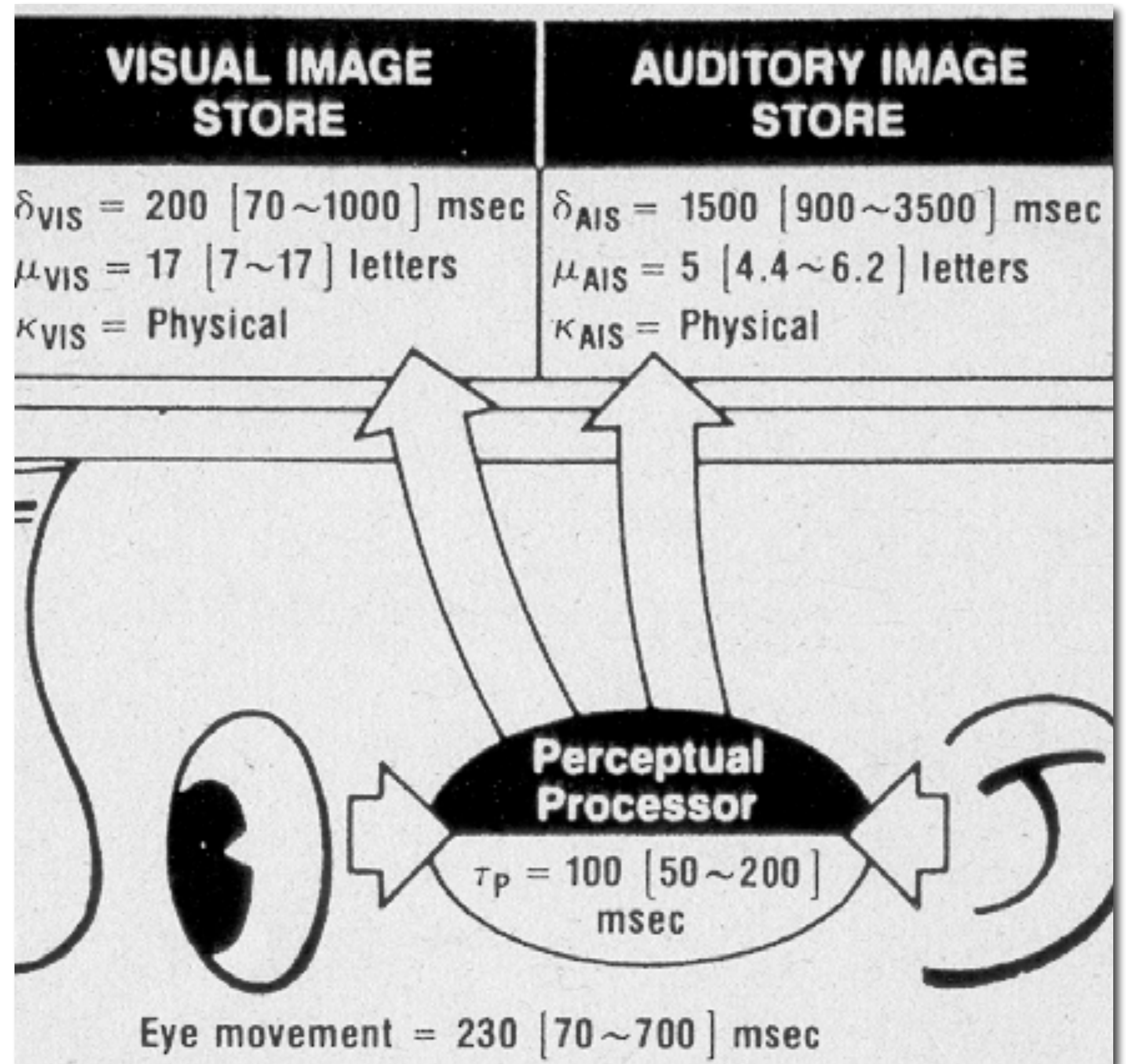
# In-Class Experiment 1: Perceptual Processor

- Work in pairs of two
- Read out the text from *Experiment 1* to your group partner
- The other partner observes the eye movement of the reading person
- Then switch
- What did you observe?



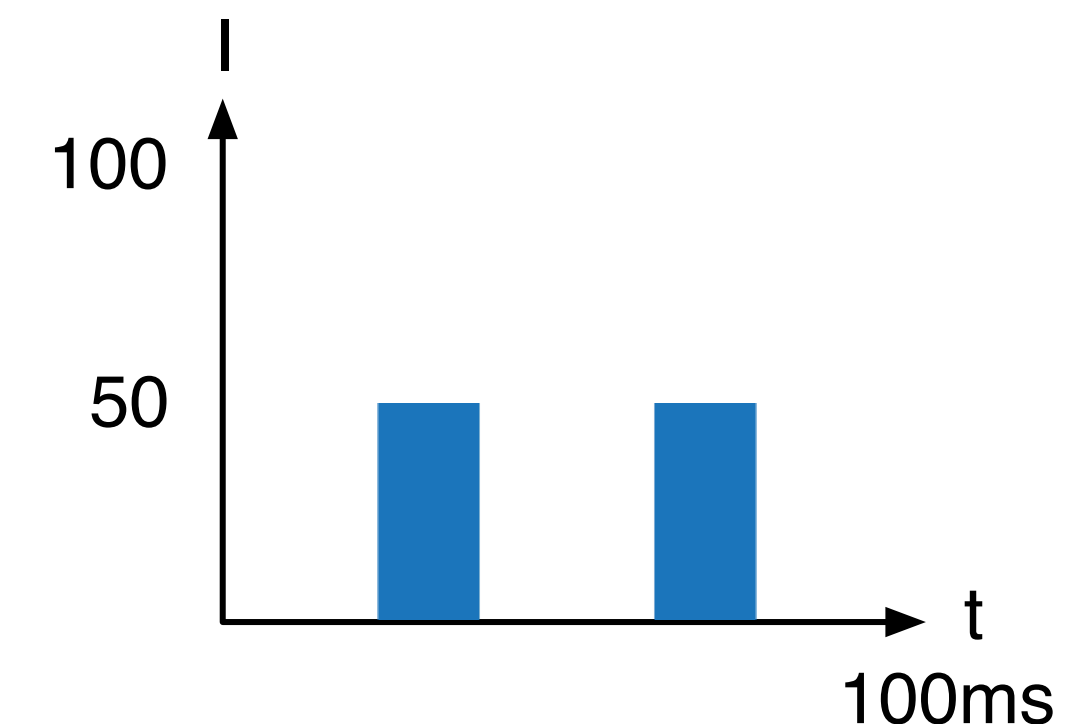
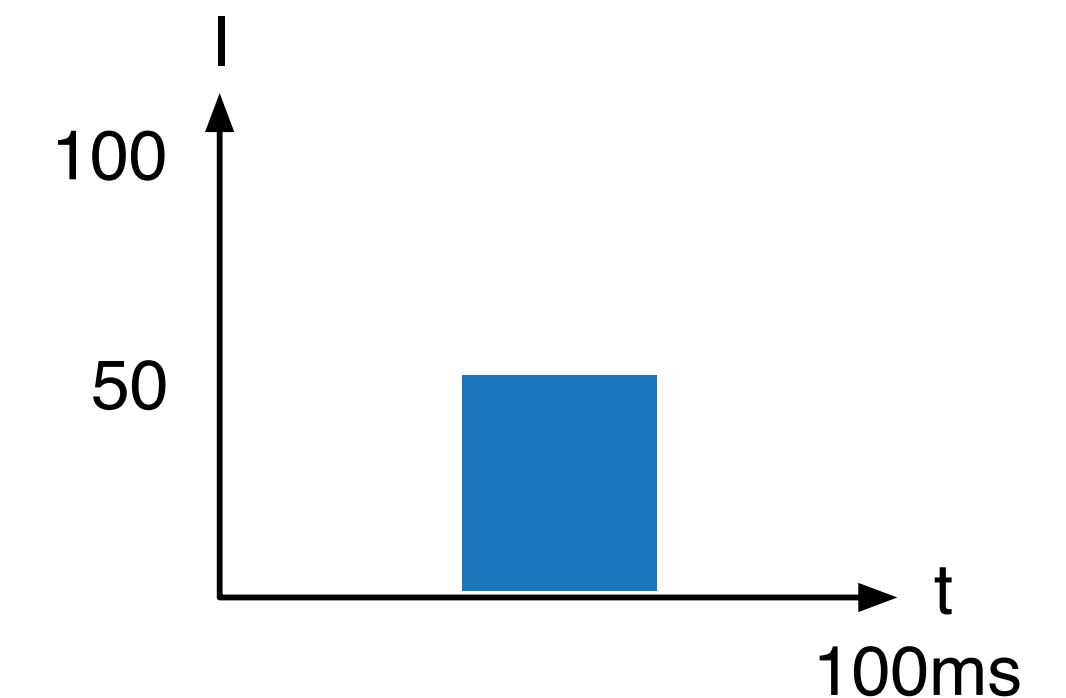
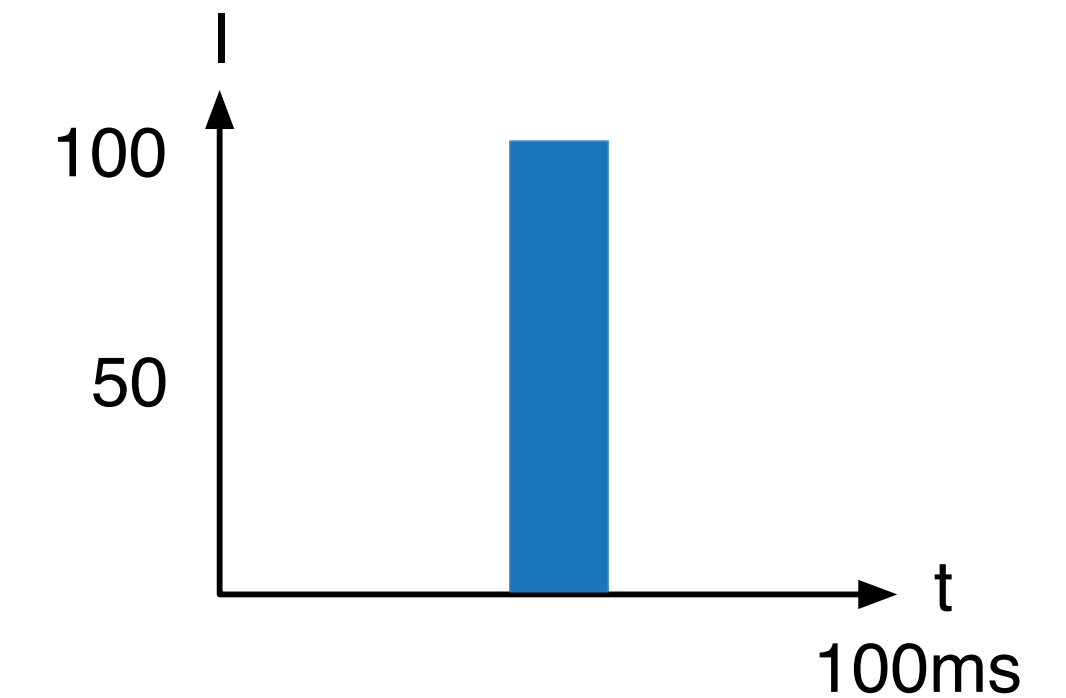
# Perception

- Eye saccades: 230 ms
- Explains reading rates
  - Maximum: 13 characters/saccade  
⇒ 652 words/minute



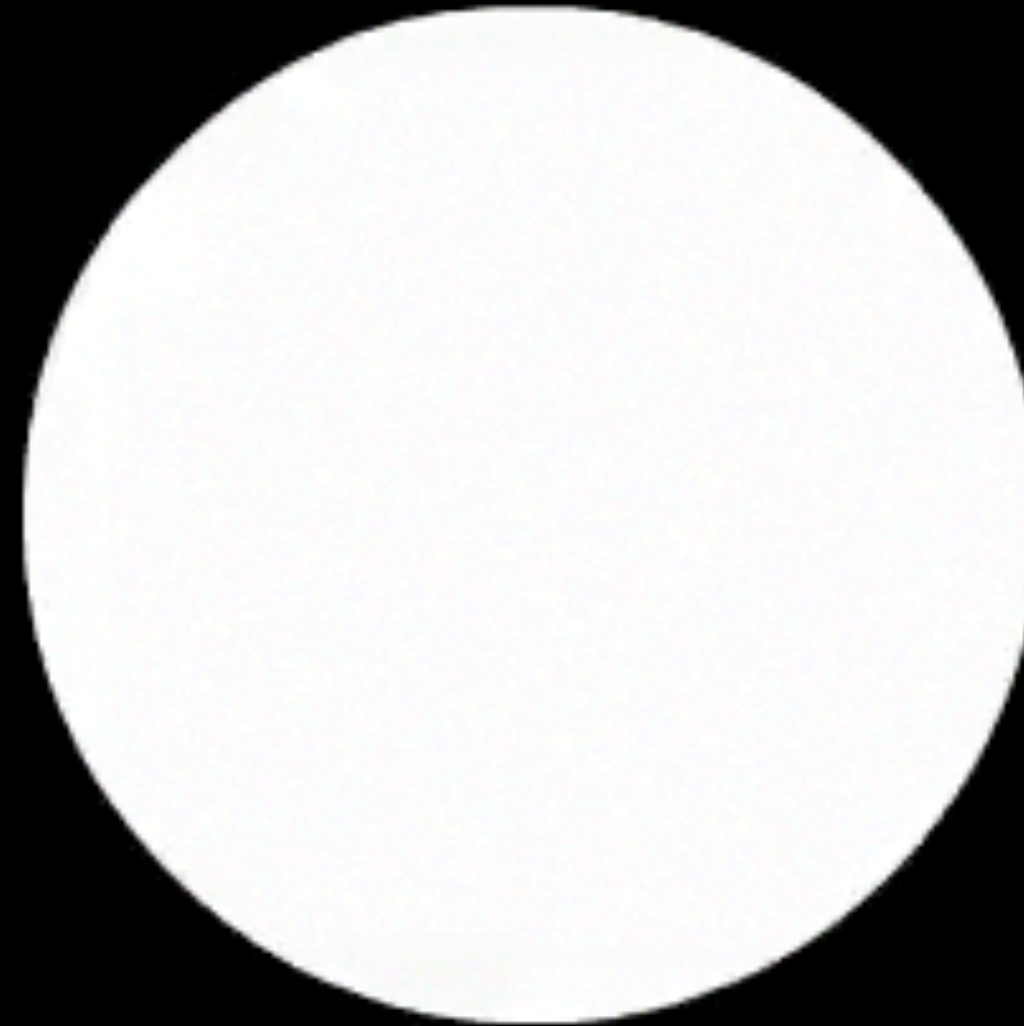
# Perceptual Processor

- Stores sensor signals in visual & auditory stores
- Perception time:  $\tau_P \approx 100 \text{ ms}$ 
  - Explains Bloch's Law
    - $R = I \times t$
    - R is response
    - I is intensity
    - t is exposure time
  - Constant response for  $t < 100\text{ms}$



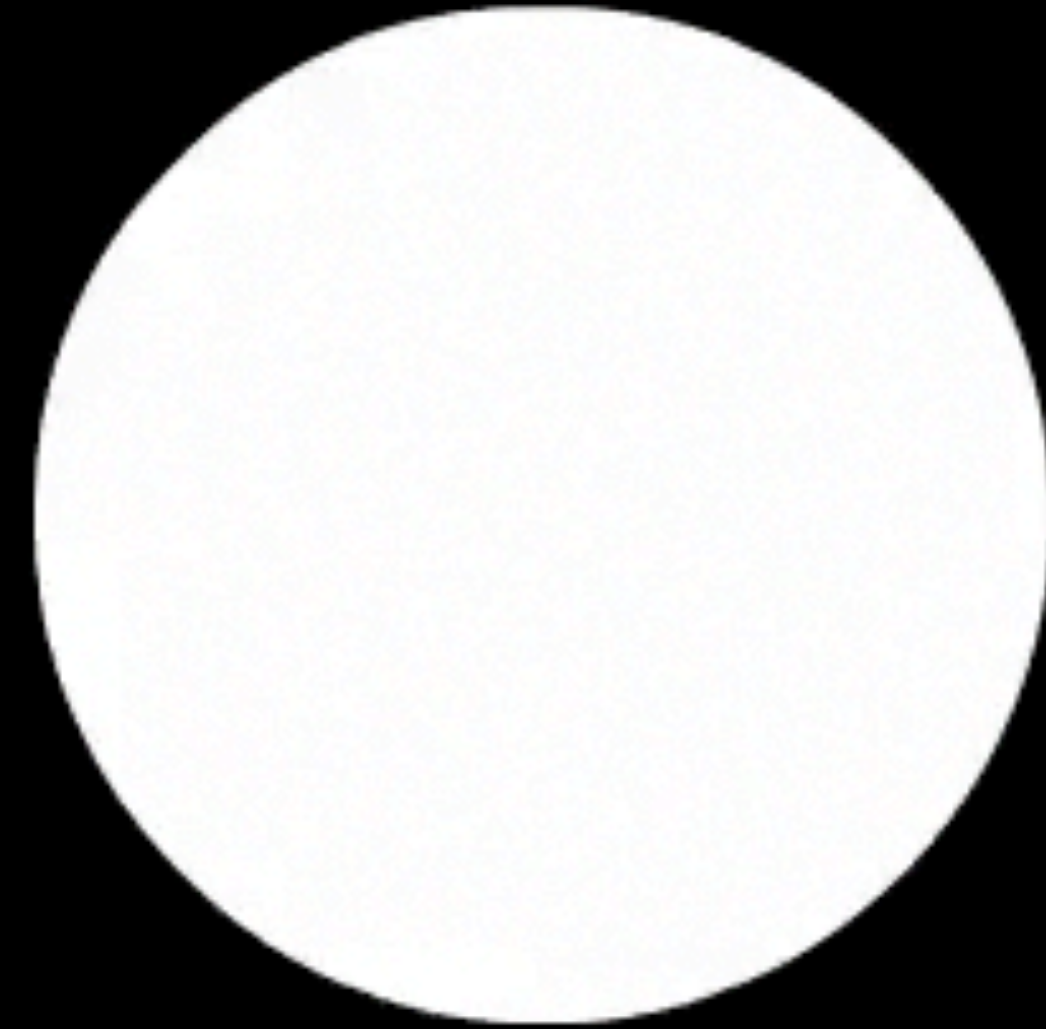
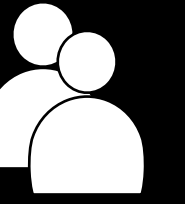


# In-Class Experiment: Bloch's Law



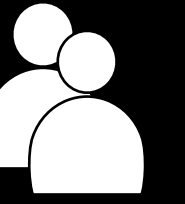
**A**

# In-Class Experiment: Bloch's Law



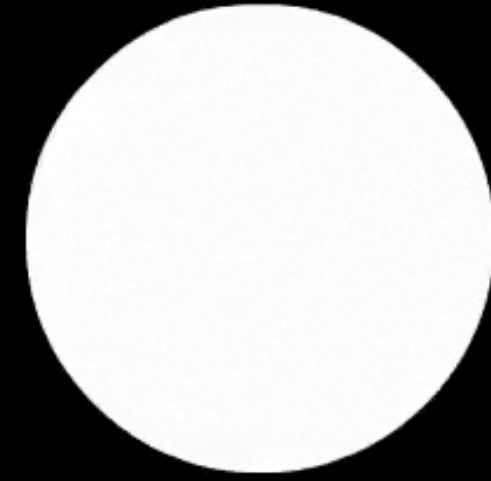
**B**

# In-Class Experiment: Bloch's Law



C

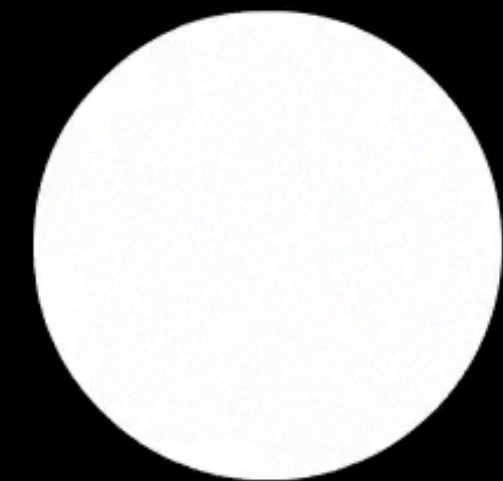




**A: 0 ms delay**



**B: 50 ms delay**

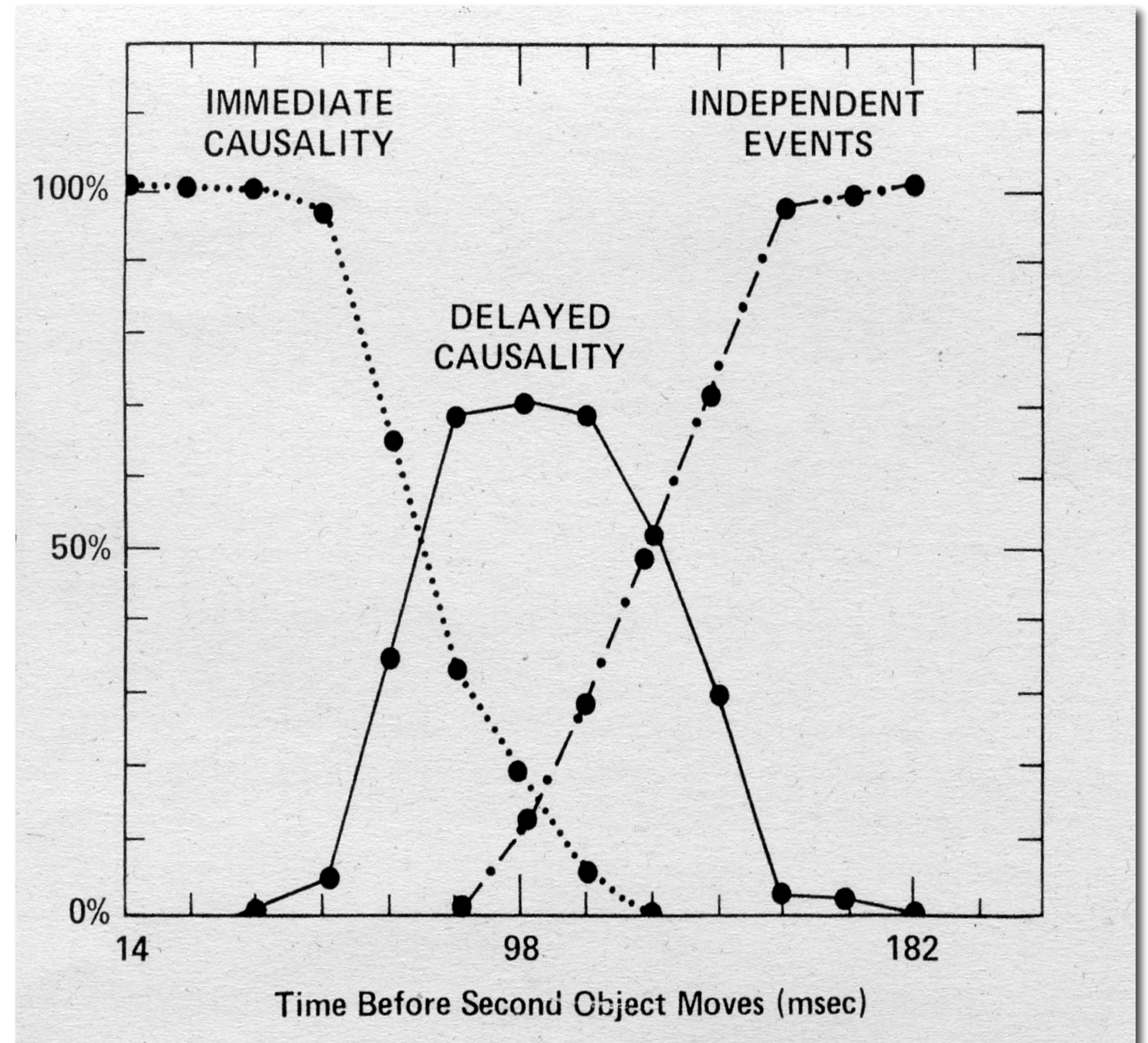


**C: 100 ms delay**

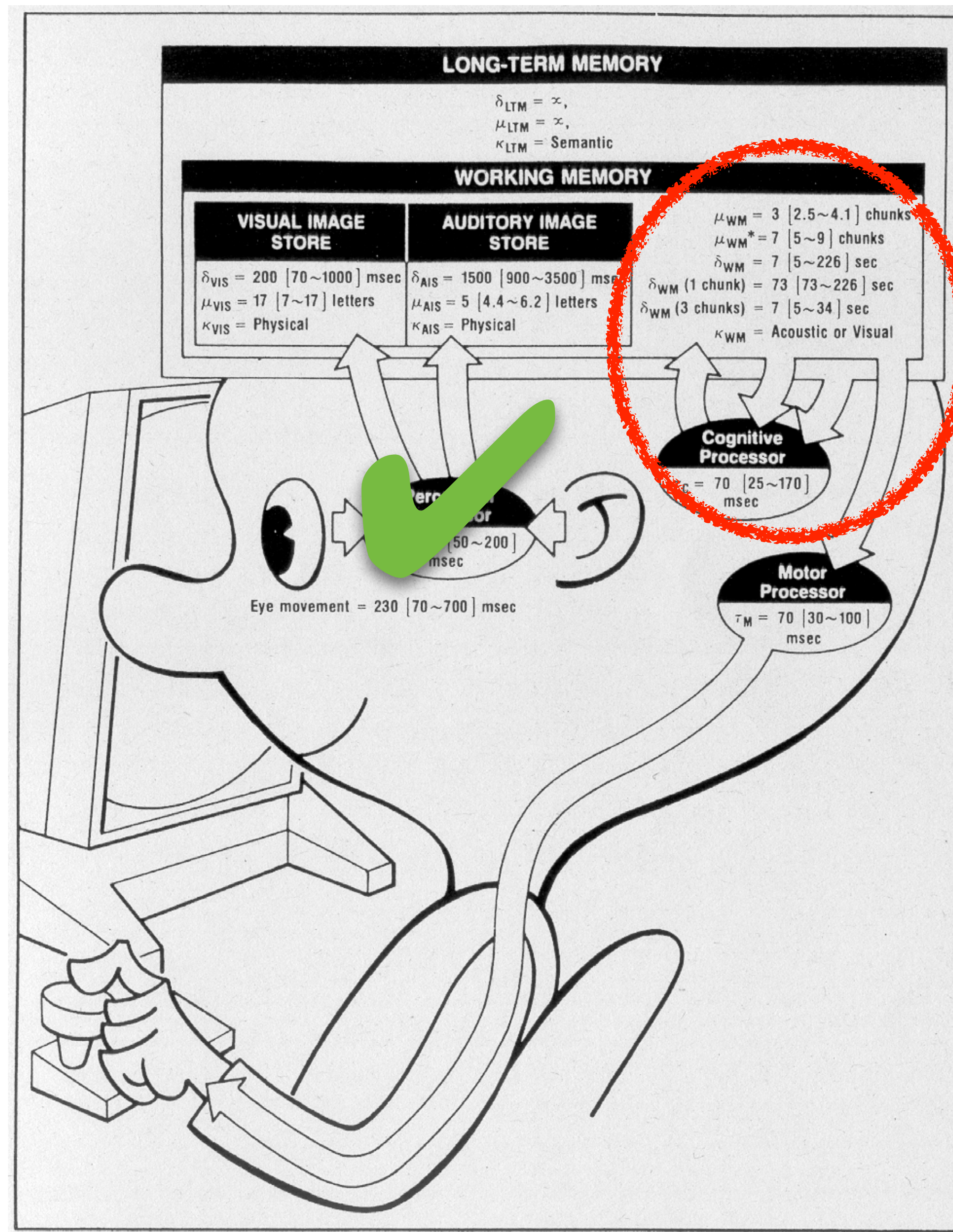


# Perceptual Processor

- Perception time:  $\tau_P \approx 100$  ms
  - Explains animation rates (10 fps for “MiddleMan”)
  - Explains max. delay before causality breaks down
  - Shortens with intensity









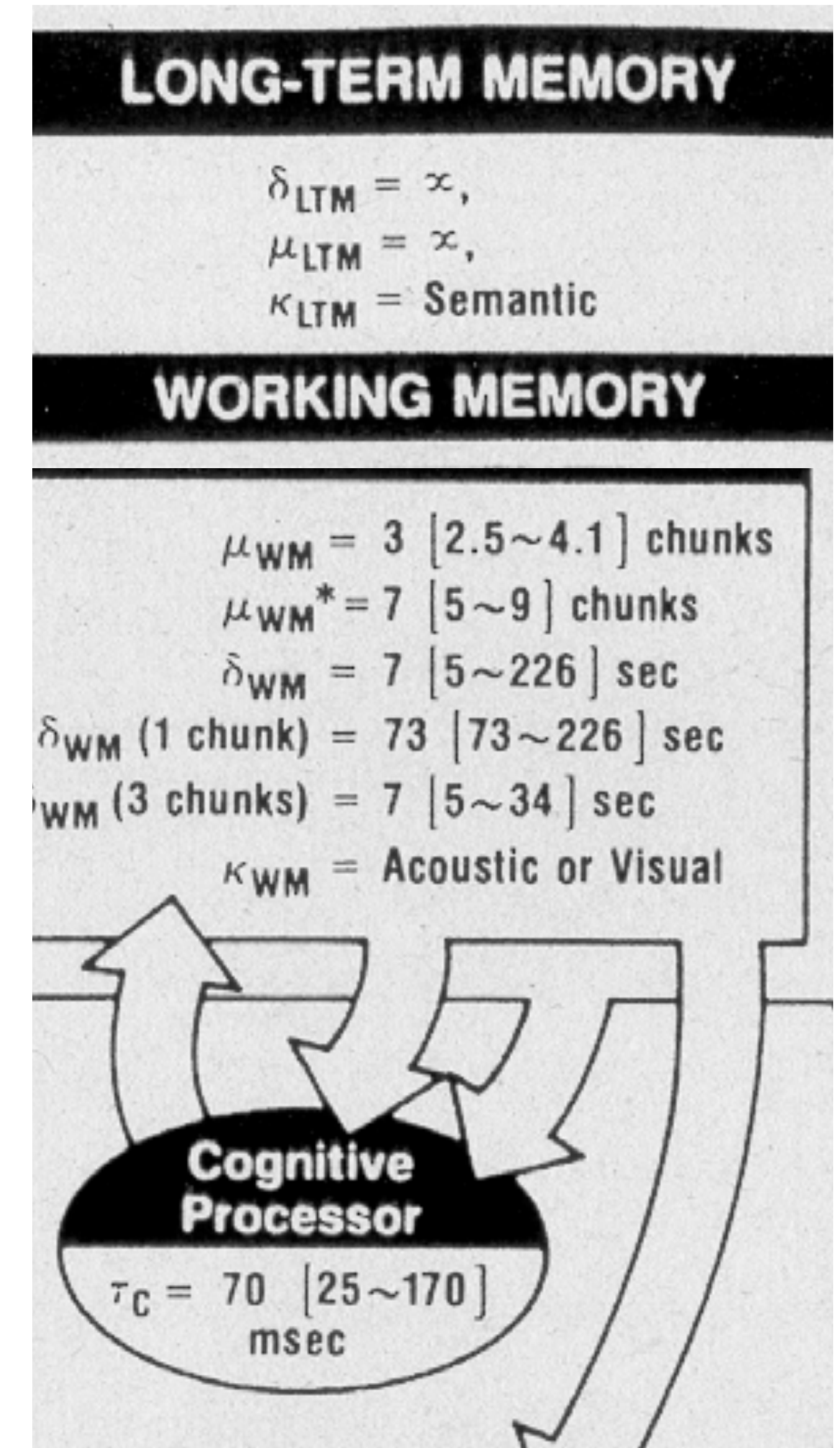
# In-Class Experiment 2: Cognitive System



- As a group of two
  - One of you (P1) reads out a random sequence of 5 digits from your sheet to the other (P2)
  - Then P2 counts backwards aloud from 50
  - Then P1 asks P2 another question (like what they had for dinner three days ago?)
  - Then P2 writes down the numbers that they still remember.
- Switch roles, repeat with 9 digits.
- Finally, switching roles again, read the long sequence of numbers to your partner, stopping somewhere suddenly. See how many of the last numbers they can repeat immediately.

# Cognitive System

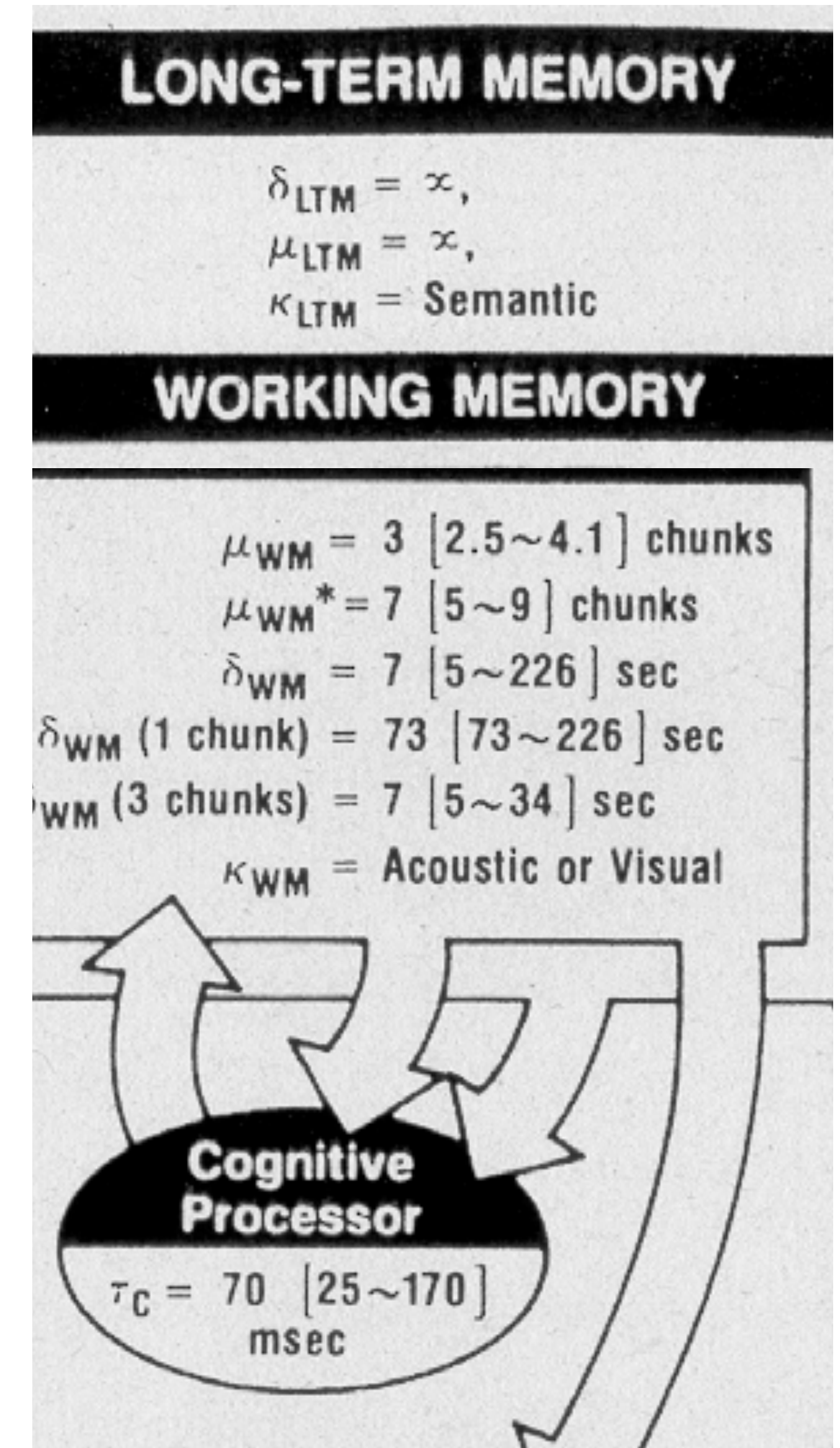
- Chunks depend on user & task
- Working memory:
  - Capacity:  $\mu_{WM} = 7 \pm 2$  chunks (Miller '56)
  - Half life:  $\delta_{1,WM} = 73$  s (1 chunk)  
 $\delta_{3,WM} = 7$  s (3 chunk)
  - Visual/acoustic encoding
- In 2001, Nelson Cowen showed that  $\mu_{WM}$  is actually  $4 \pm 1$  chunks.





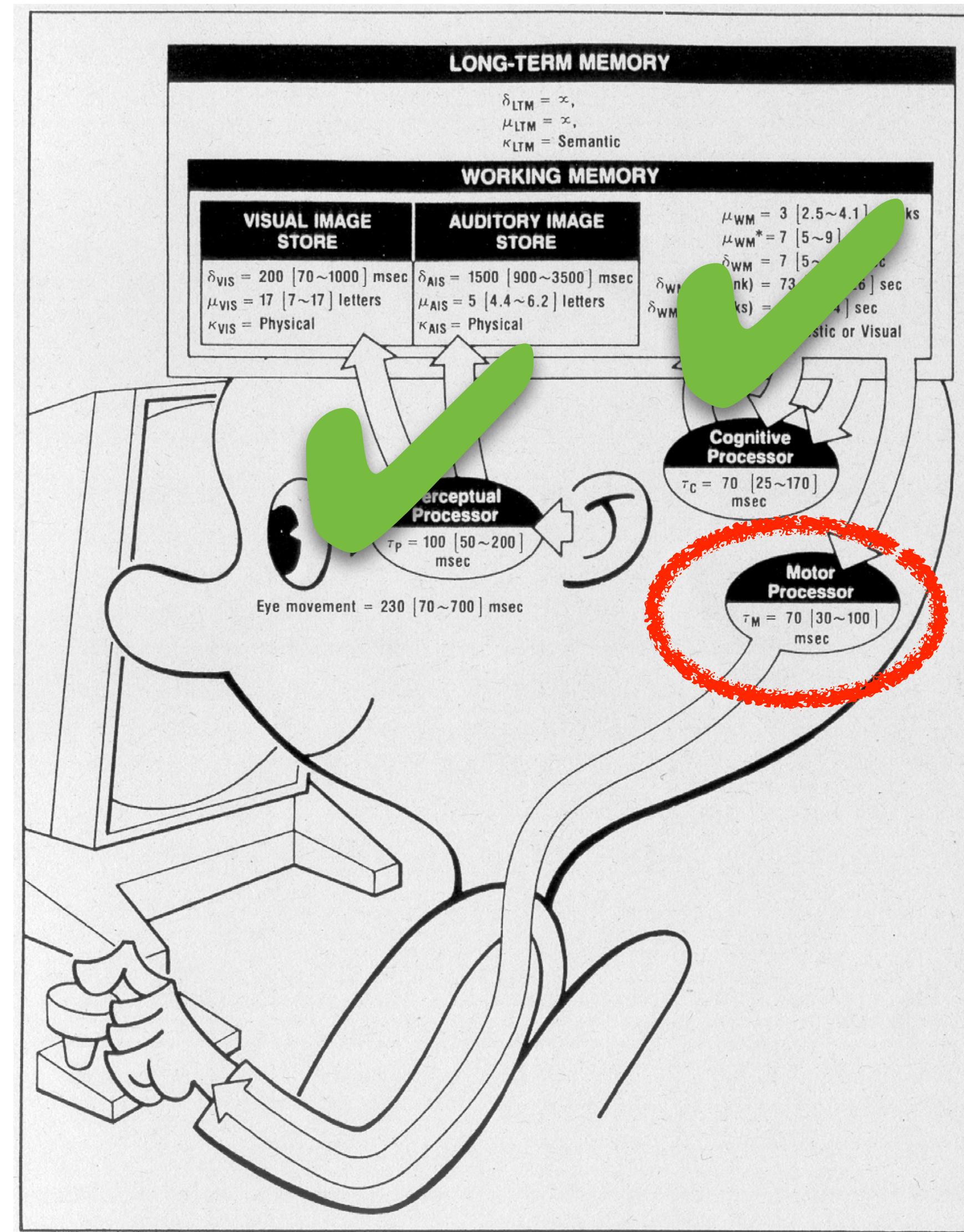
# Cognitive System

- Cognitive processor:
    - Processing time  $\tau_C = 70 \text{ ms}$
  - Long-term memory:
    - Infinite capacity and half life
    - Semantic encoding (associations)
    - Fast read, slow write
- ⇒ Remembering items maxes out at 7 s/chunk learning speed (1 pass)





# Model Human Processor

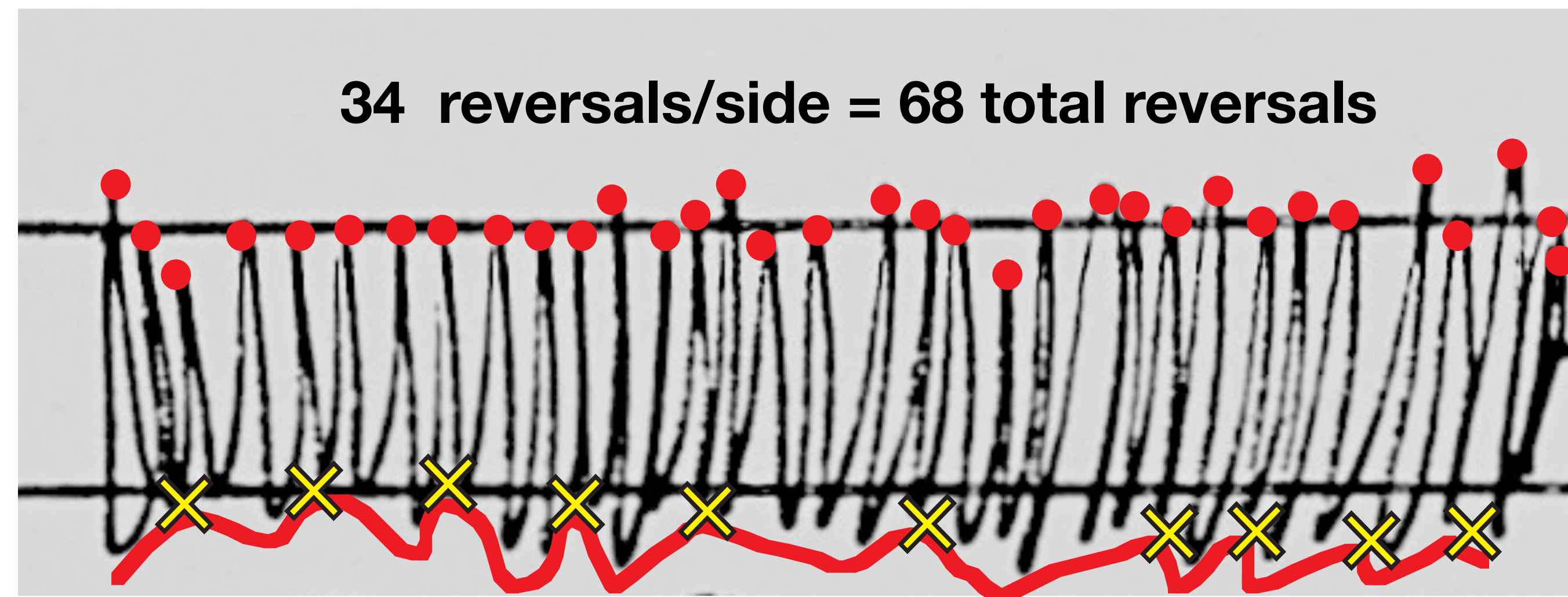




# In-Class Experiment 3: Motor System



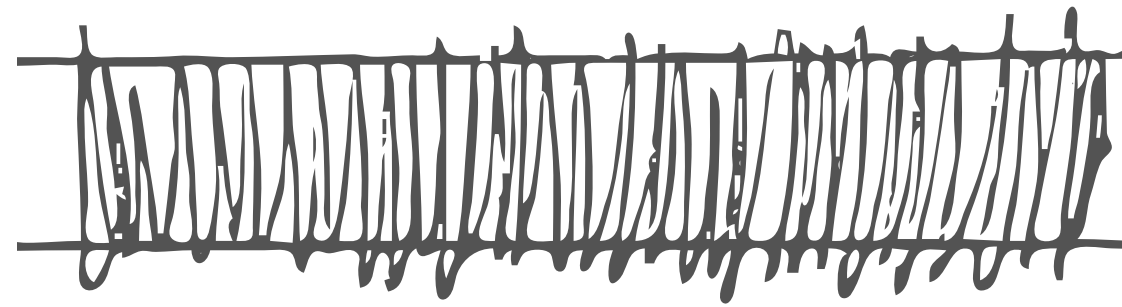
- Experiment: draw strokes between lines for 5s. Try to reach both lines.
- Count number of reversals
  - How many milliseconds per reversal?
- Create a contour of stroke bottoms, count number of corrections
  - How many milliseconds per correction?



**10 corrections/side = 20 total corrections**

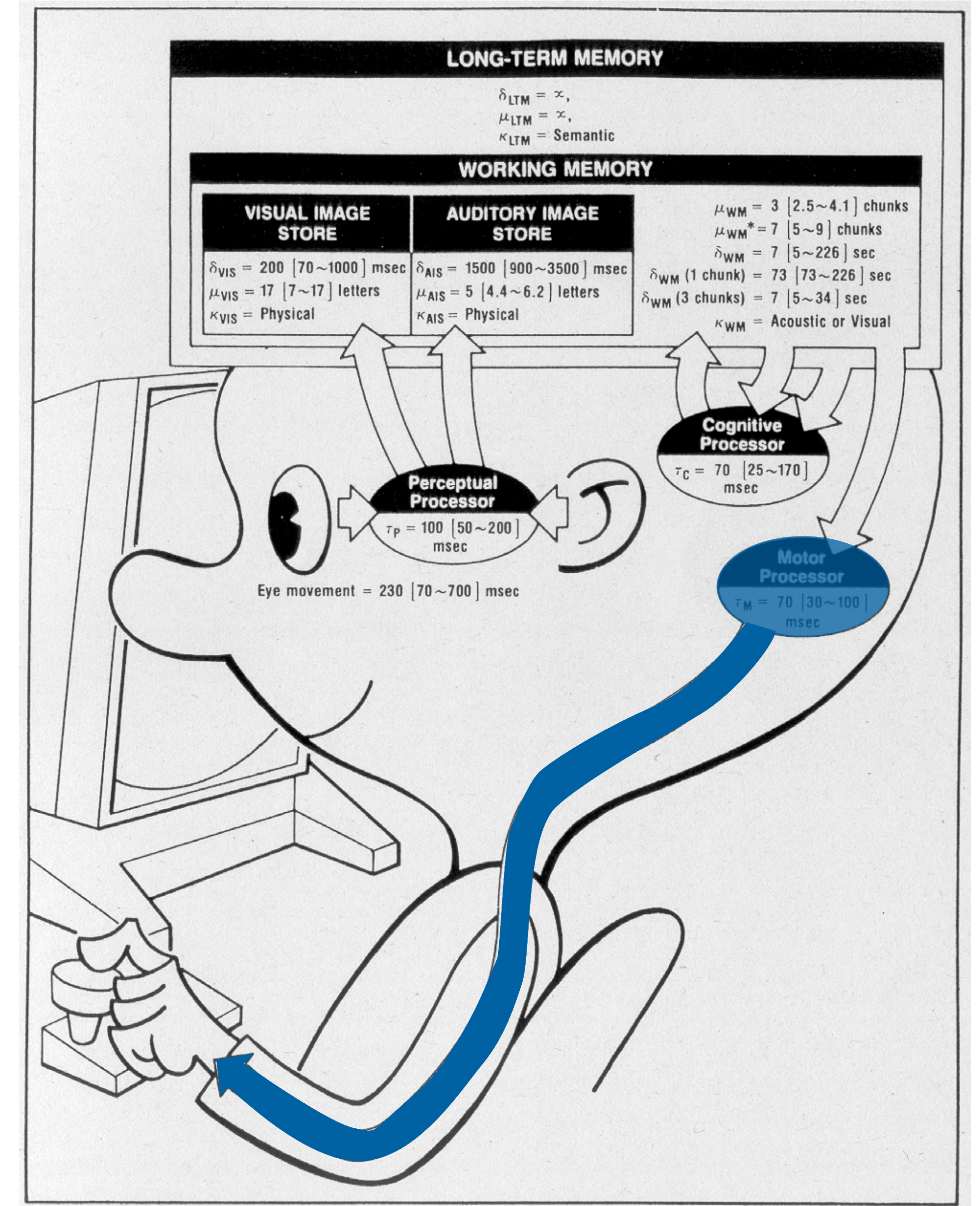
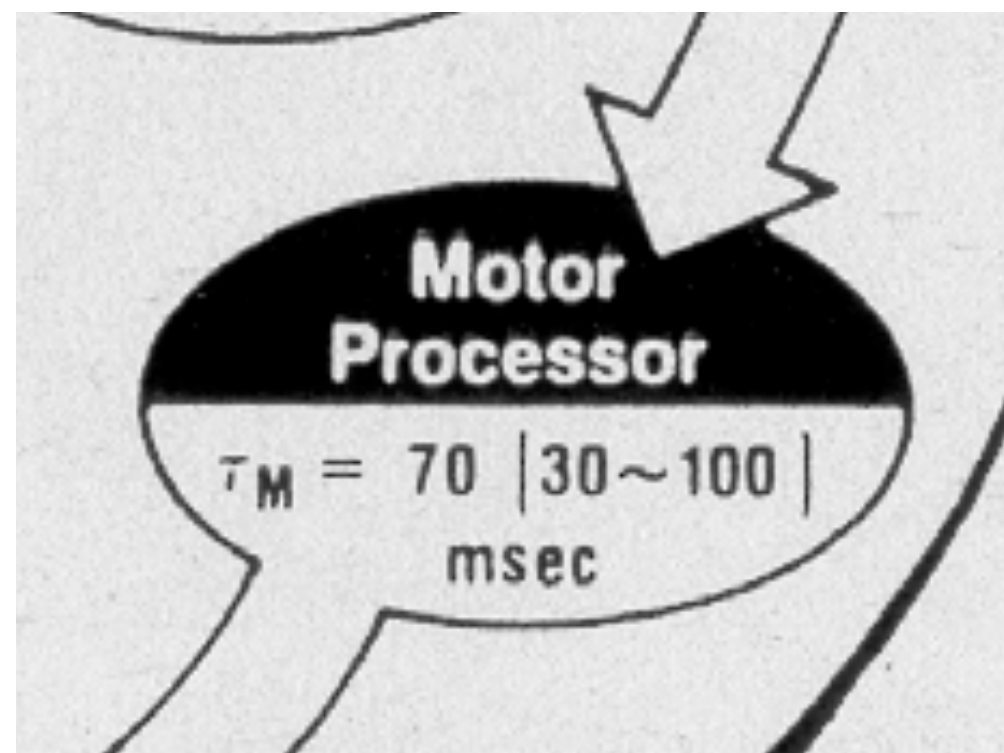


# Motor System



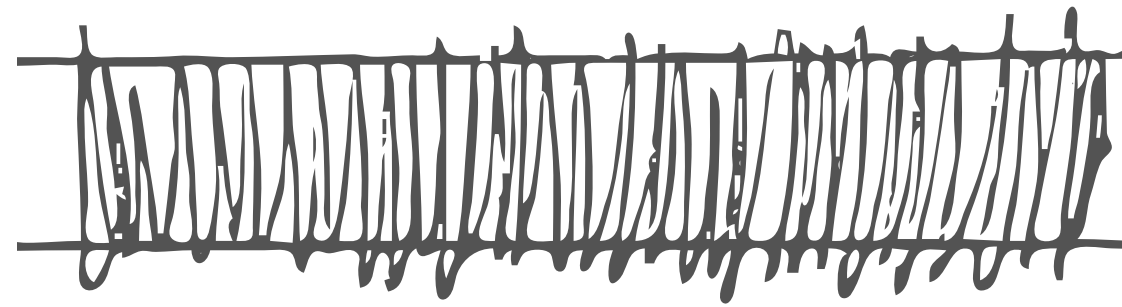
74 ms/reversal  
250 ms/correction

- Motor processor (open loop)
    - $\tau_M = 70 \text{ ms}$
- ⇒ Average time between each reversal



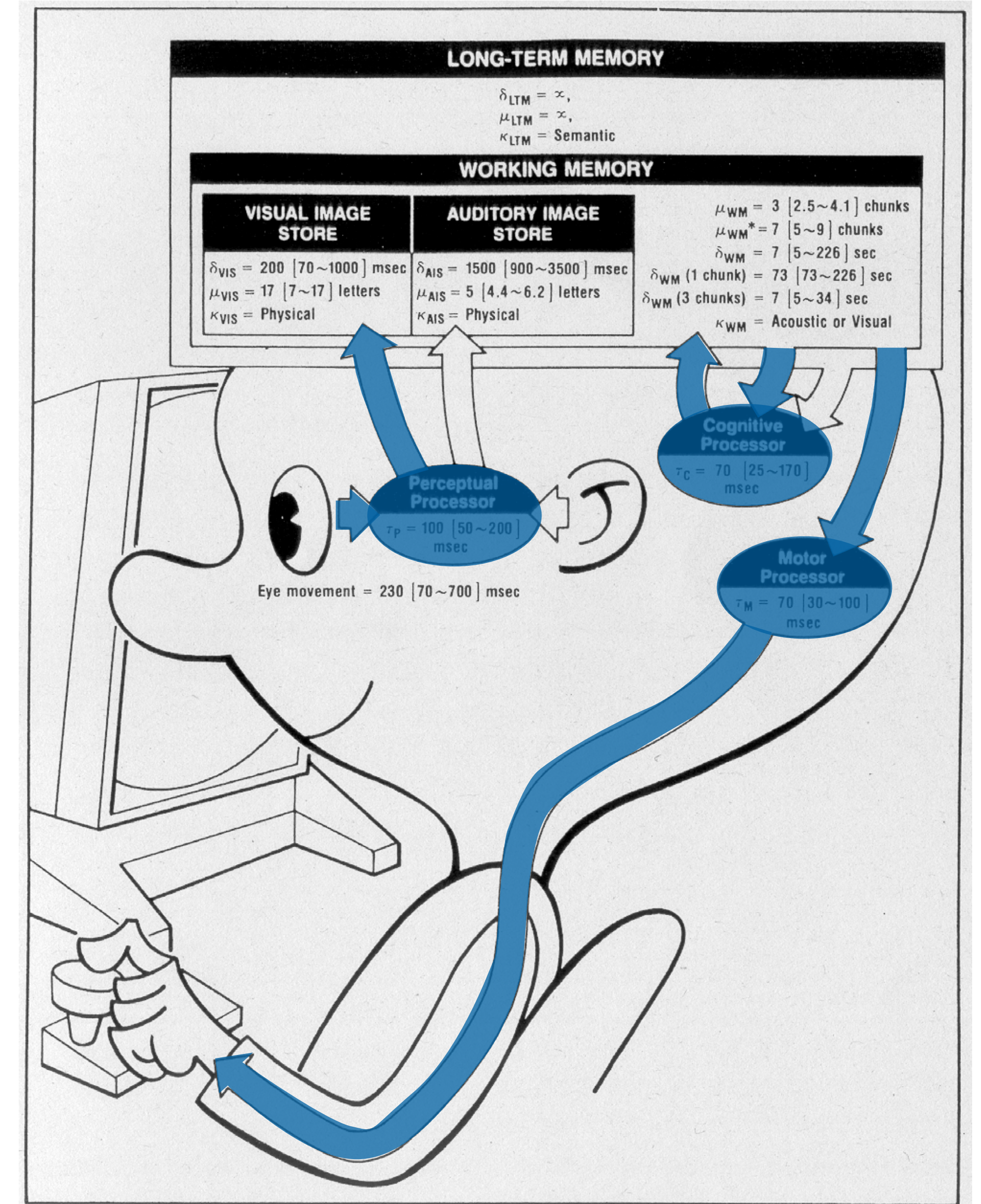


# Motor System



74 ms/reversal  
250 ms/correction

- Closed loop:
    - $\tau_P + \tau_C + \tau_M = 240 \text{ ms}$
- ⇒ Average time between each correction



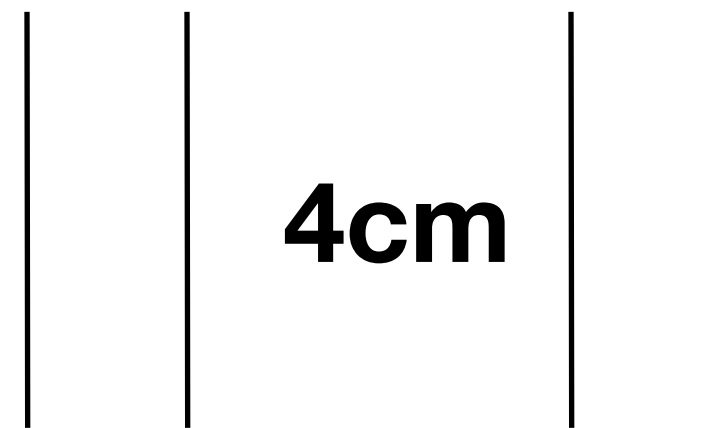


# Fitts' Law

# In-Class Experiment 5: Tapping Task

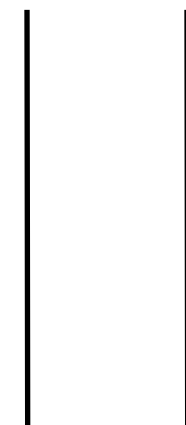


**1cm**

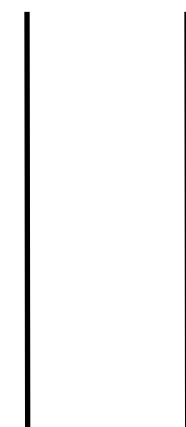
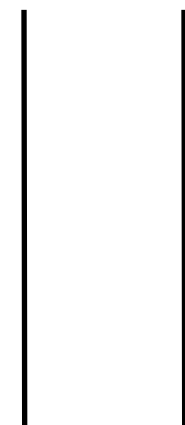


**4cm**

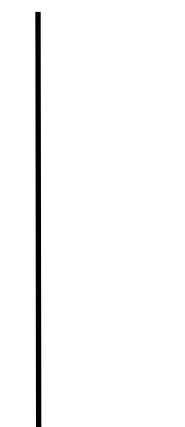
Same for 0.5 cm and 2 cm wide strips  
Tap for 10 s, count taps afterwards



**8cm**

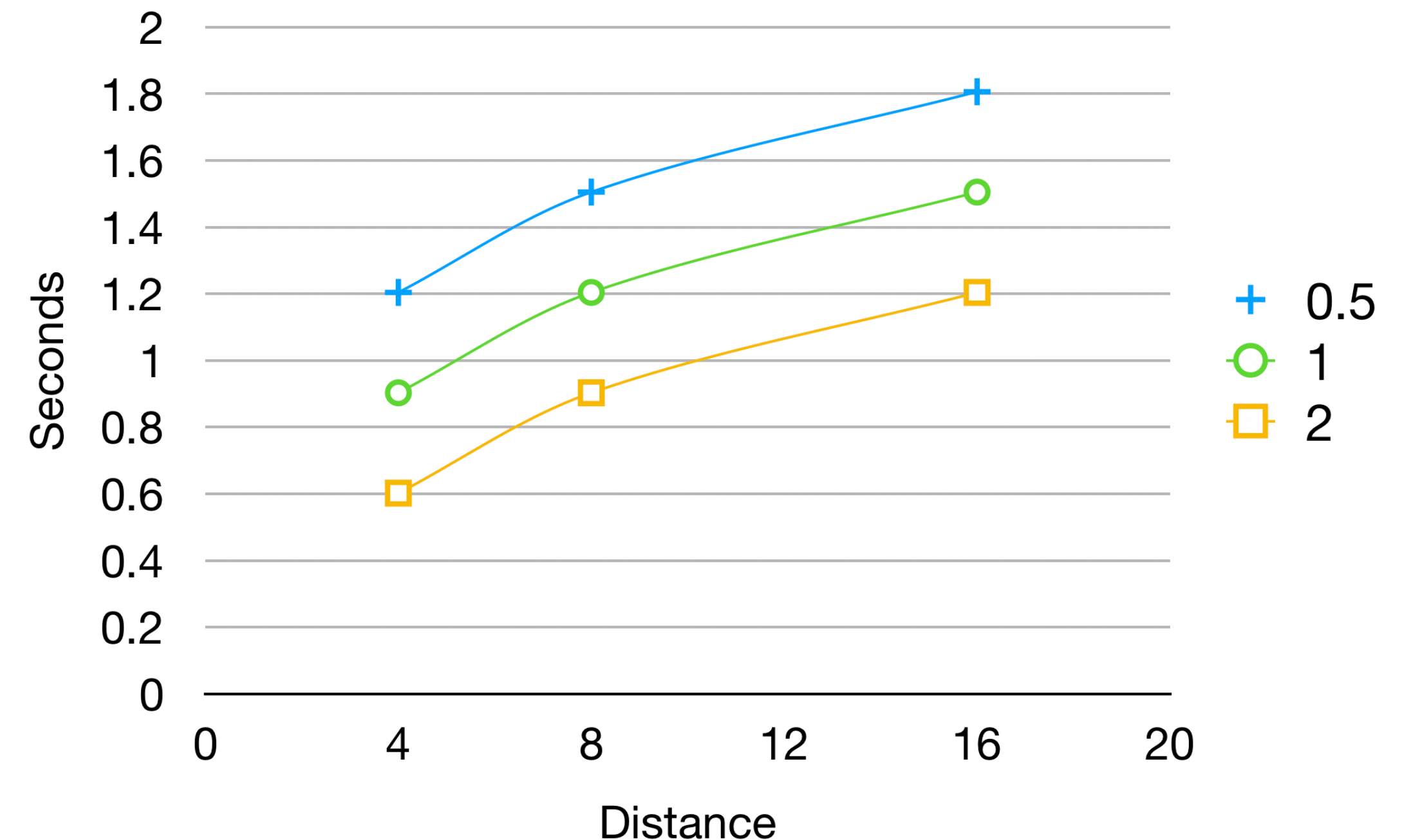


**16cm**



# Tapping Task Results

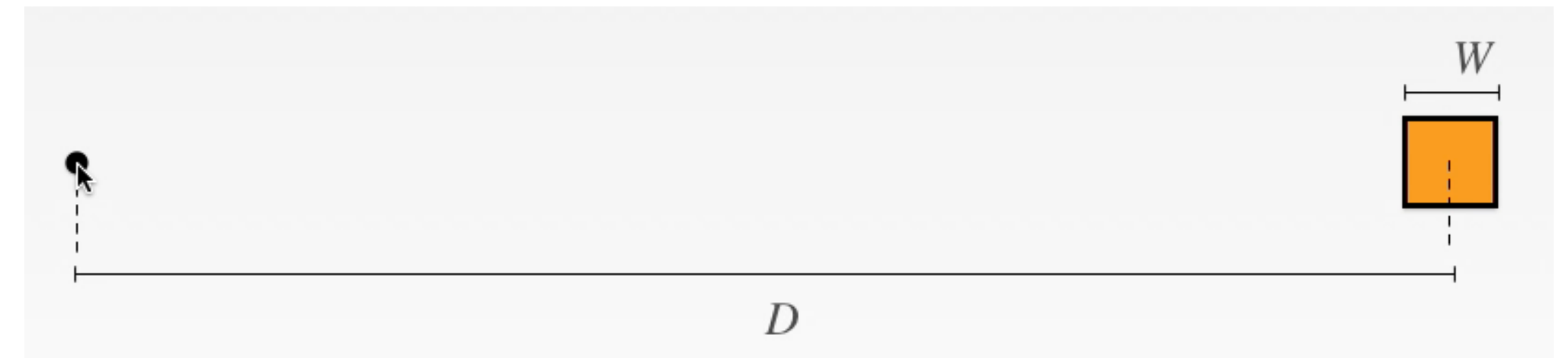
- Doubling the distance adds roughly a constant to execution time  
⇒ indicates logarithmic nature
- Doubling the target width (W) gives about same results as halving the distance (D)  
⇒ indicates connection of  $D/W$  in formula





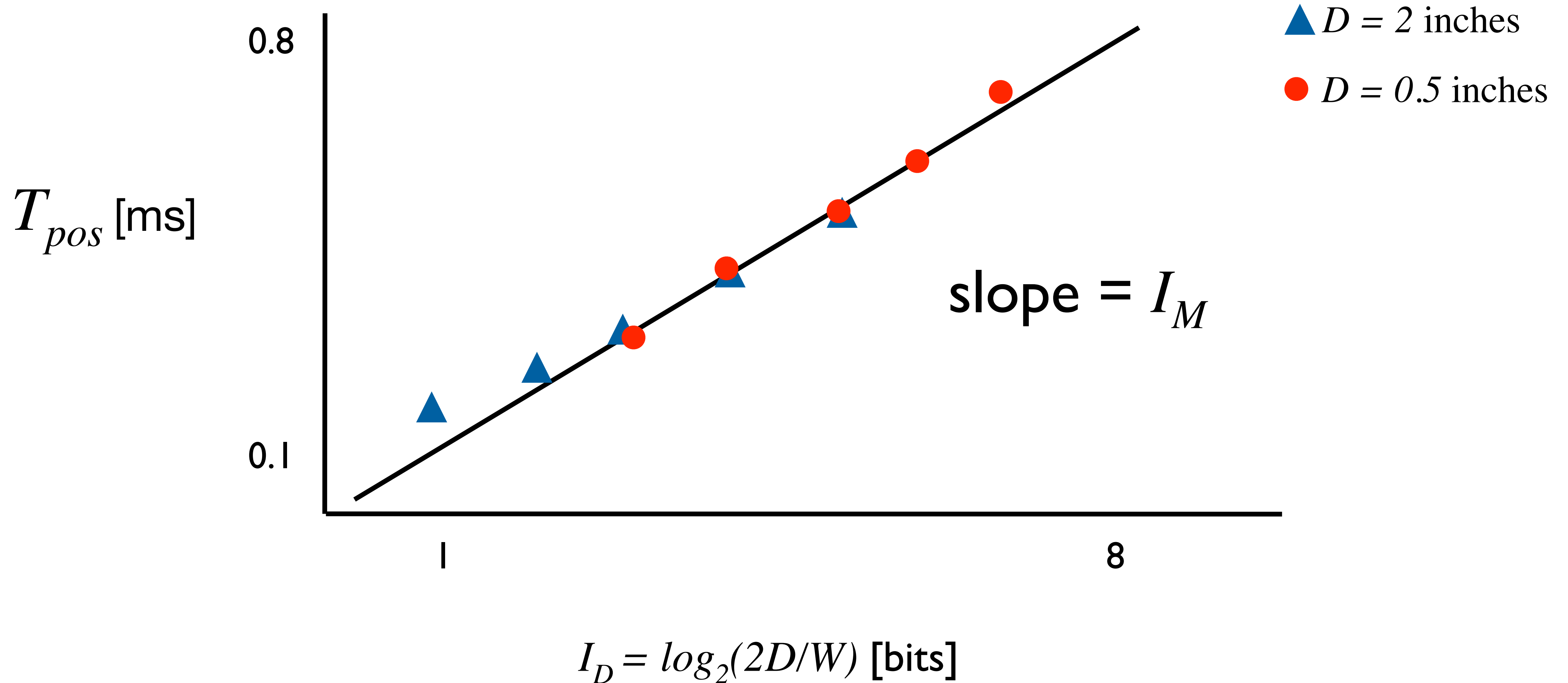
# Motor System: Fitts' Law

- Goal: Predict time to press buttons (physical or on-screen) as function of distance and size
- Result (Fitts, 1954):  $T_{pos} = I_M \cdot I_D$ 
  - $T_{pos}$  time to reach button
  - $I_M = 100$  ms/bit index of movement, constant
  - $I_D = \log_2(2D / W)$  index of difficulty, in bits
- Fitts' law can be derived from CMN model



# Visualizing Fitts' Law

Experiment: fixed distance  $D$ , varying width  $W$

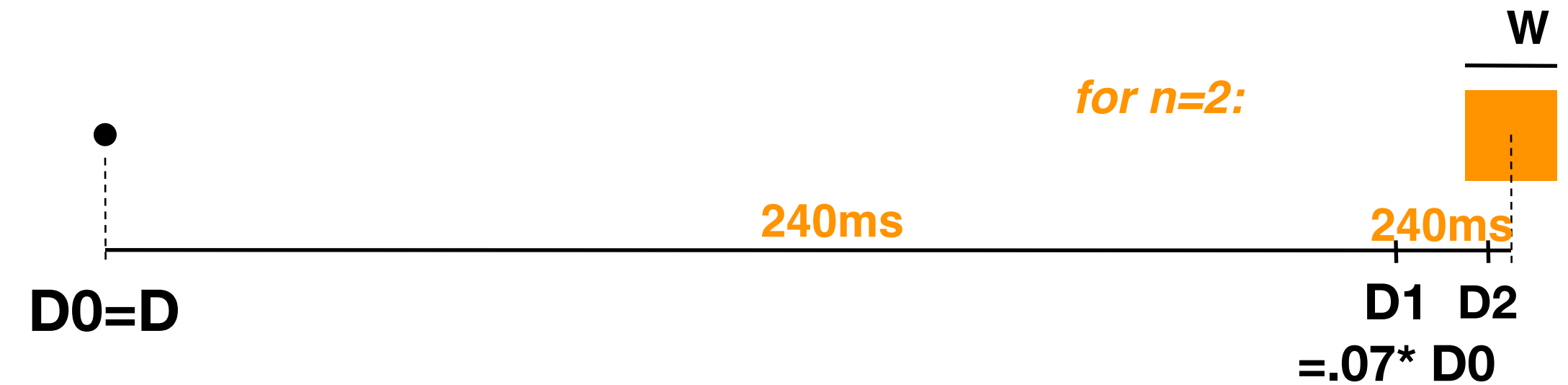




# Deriving Fitts' Law from CMN (1)

$D_i$  := remaining distance to target after  $i$  movements  
 $\epsilon := D_i / D_{i-1} < 1$  (relative movement precision, experiment shows)  
 $\epsilon = 0.07$  (constant according to CMN model)

$D_1 = \epsilon \cdot D_0 = \epsilon \cdot D$   
 $D_2 = \epsilon \cdot D_1 = \epsilon^2 \cdot D$   
 $\dots$   
 $D_n = \epsilon \cdot D_{n-1} = \epsilon^n \cdot D \leq W/2$  (hand reaches target after  $n$  movements)



$$\begin{aligned}
 \epsilon^n &\leq \frac{W}{2D} \\
 \Leftrightarrow n &\geq \log_{\epsilon} \left( \frac{W}{2D} \right) \quad (\log \text{ for base } < 1 \text{ turns inequality sign}) \\
 \Leftrightarrow n &\geq \frac{\log_2 \left( \frac{W}{2D} \right)}{\log_2 \epsilon} \\
 \Leftrightarrow n &\geq -\frac{\log_2 \left( \frac{2D}{W} \right)}{\log_2 \epsilon}
 \end{aligned}$$

# Deriving Fitts' Law from CMN (2)

Total positioning time is  $T_{pos} = n \cdot (t_{WP} + t_{KP} + t_{MP})$

Insert  $n$  to arrive at Fitts' Law:

$$\begin{aligned} T_{pos} &= -\frac{\log_2 \left( \frac{2D}{W} \right)}{\log_2 \epsilon} \cdot (t_{WP} + t_{KP} + t_{MP}) && \text{(rearrange)} \\ &= -\frac{(t_{WP} + t_{KP} + t_{MP})}{\log_2 \epsilon} \cdot \log_2 \left( \frac{2D}{W} \right) \\ &= -\frac{240 \text{ ms}}{\log_2 (0.07)} \cdot \log_2 \left( \frac{2D}{W} \right) && \text{(240 ms is CMN estimate)} \\ &\approx 100 \text{ ms} \cdot \log_2 \left( \frac{2D}{W} \right) \\ &= I_M \cdot I_D && \text{q.e.d.} \end{aligned}$$



# Improvements

- Welford's Formulation, 1968:

$$T_{pos} = I_M \cdot \log_2 \left( \frac{D}{W} + \frac{1}{2} \right)$$

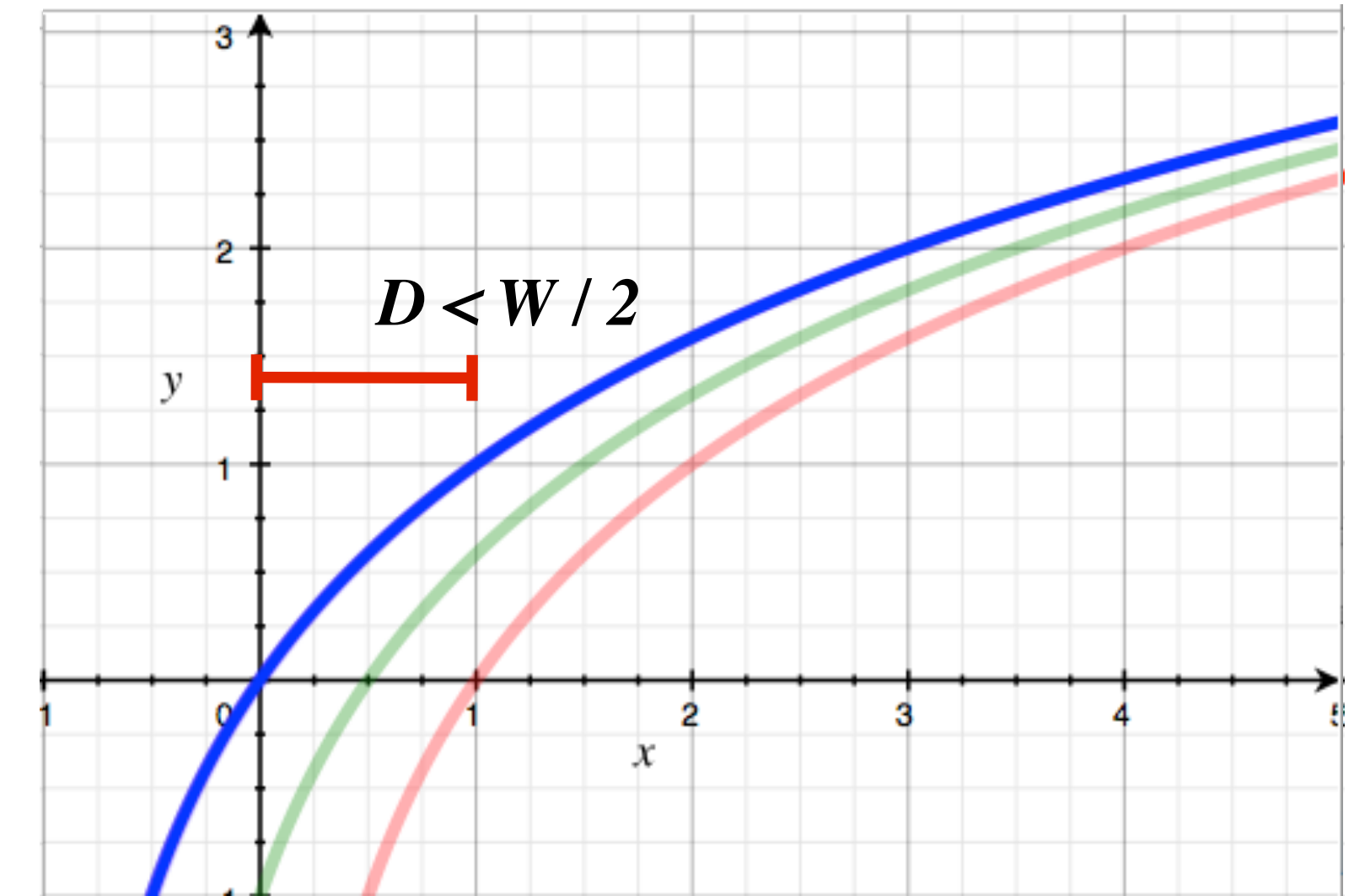
- Shannon's Formulation, ISO, 80's:

$$T_{pos} = a + b \cdot \log_2 \left( \frac{D}{W} + 1 \right)$$

- $a, b$  depend on device, determine experimentally

Use  $a = 0 \text{ ms}$ ,  $b = I_M = 100 \text{ ms}$  for quick and dirty estimates

Improved curve fit, no negative times for infinite-size targets

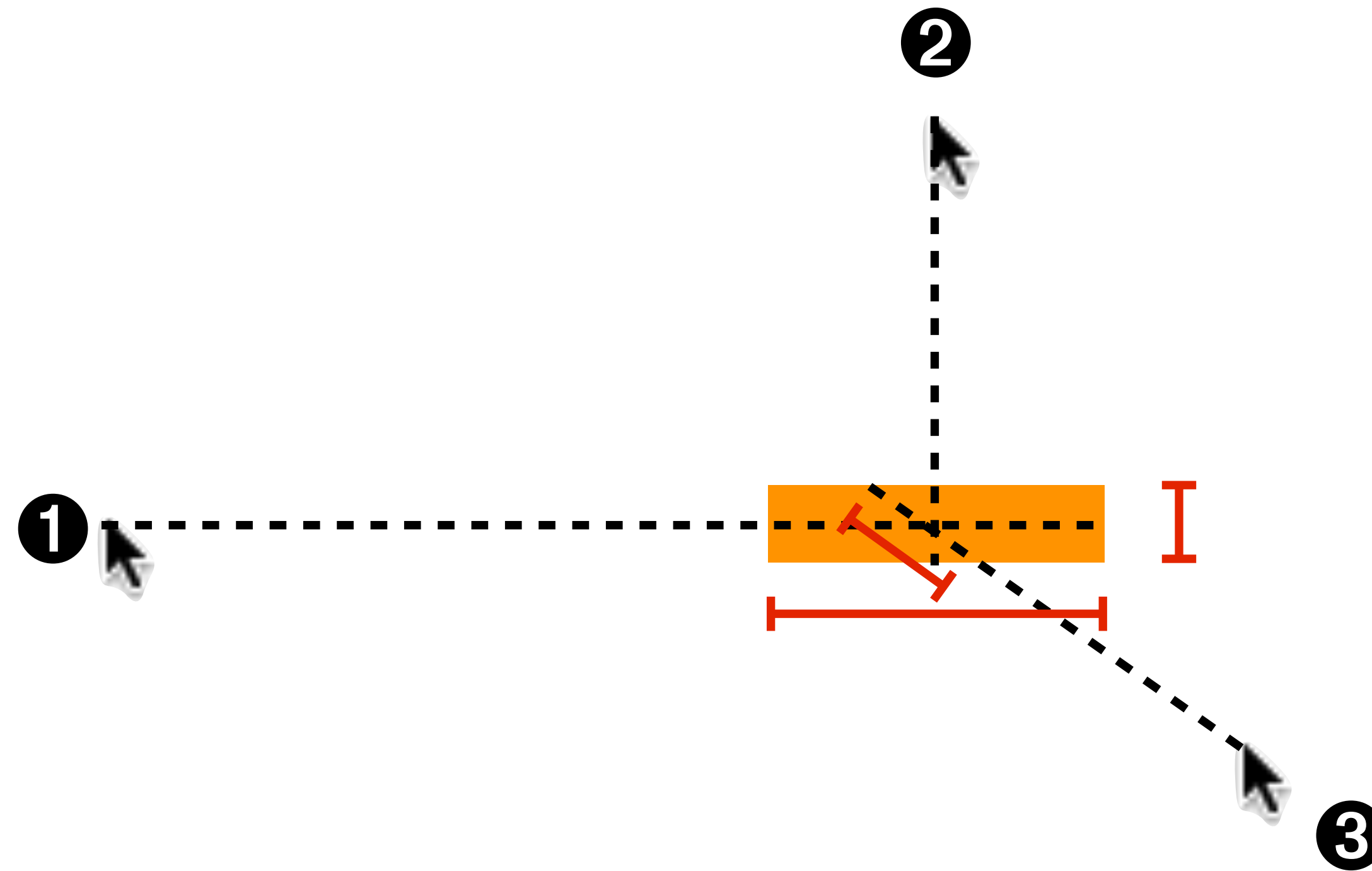


—  $T_{pos} = I_M \cdot \log_2 \left( \frac{2D}{W} \right)$

—  $T_{pos} = I_M \cdot \log_2 \left( \frac{D}{W} + \frac{1}{2} \right)$

—  $T_{pos} = a + b \cdot \log_2 \left( \frac{D}{W} + 1 \right)$

# Target Width



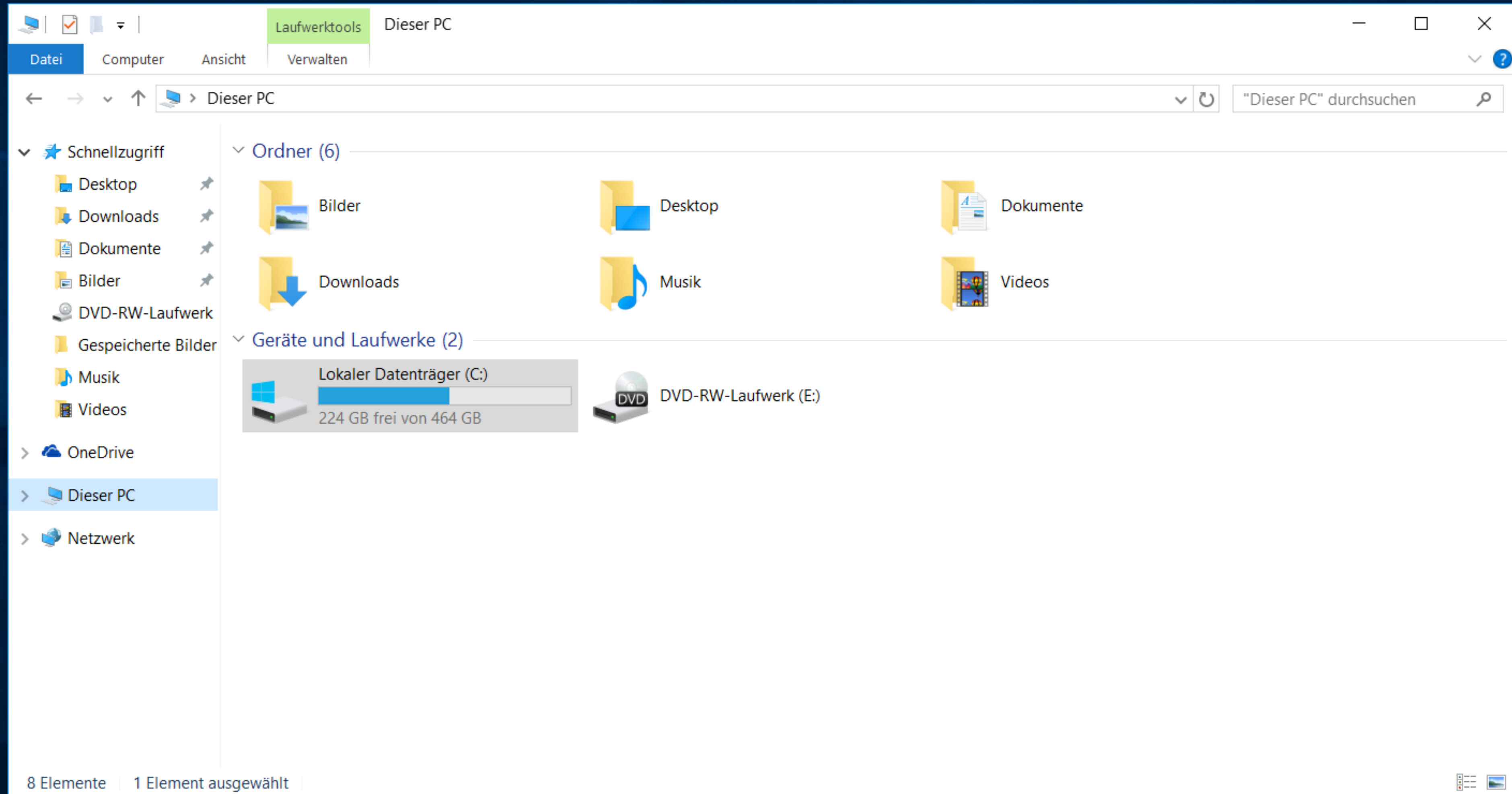
[MacKenzie & Buxton, CHI'92]



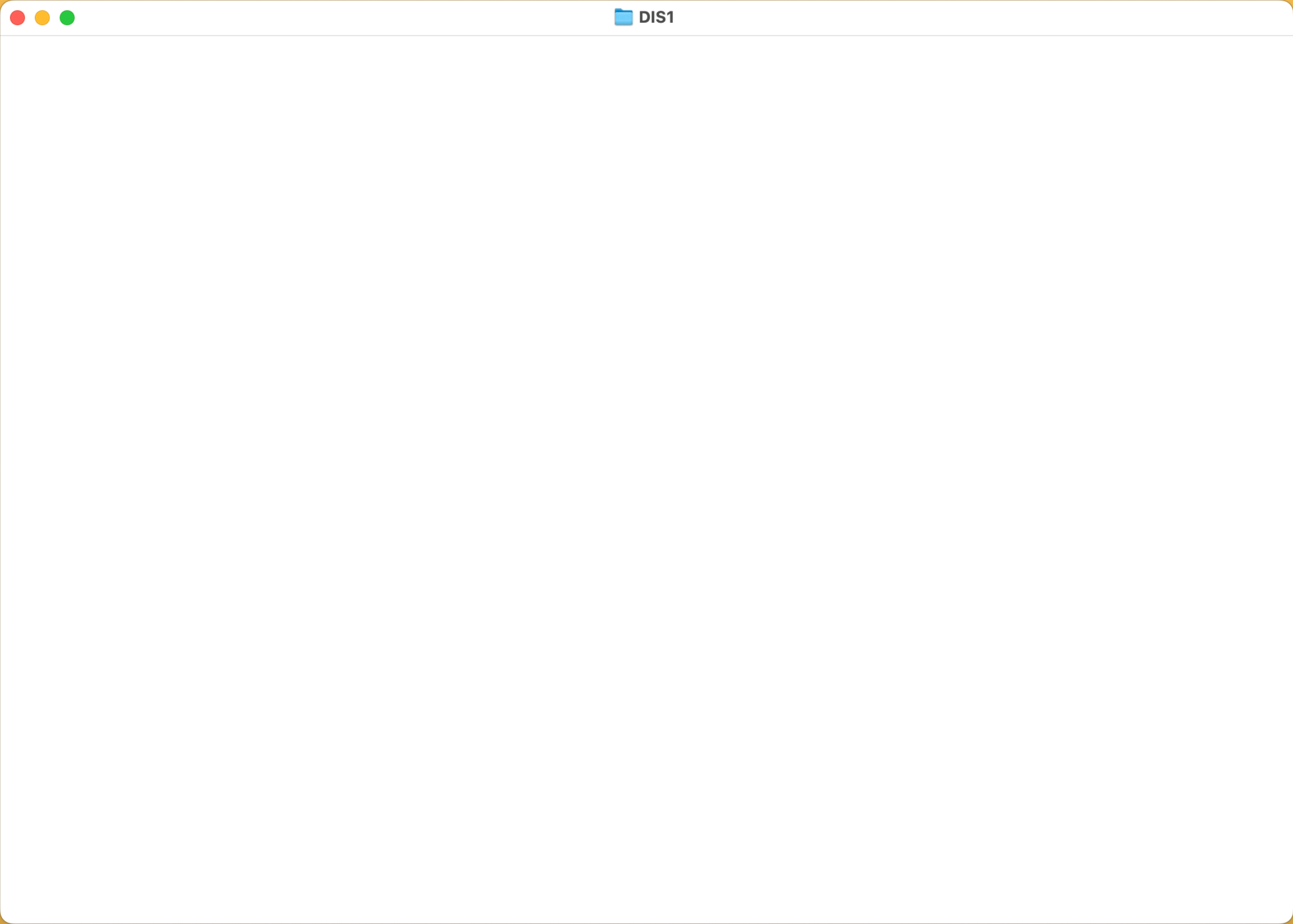


Papierkorb

# Windows 10



# macOS Monterey

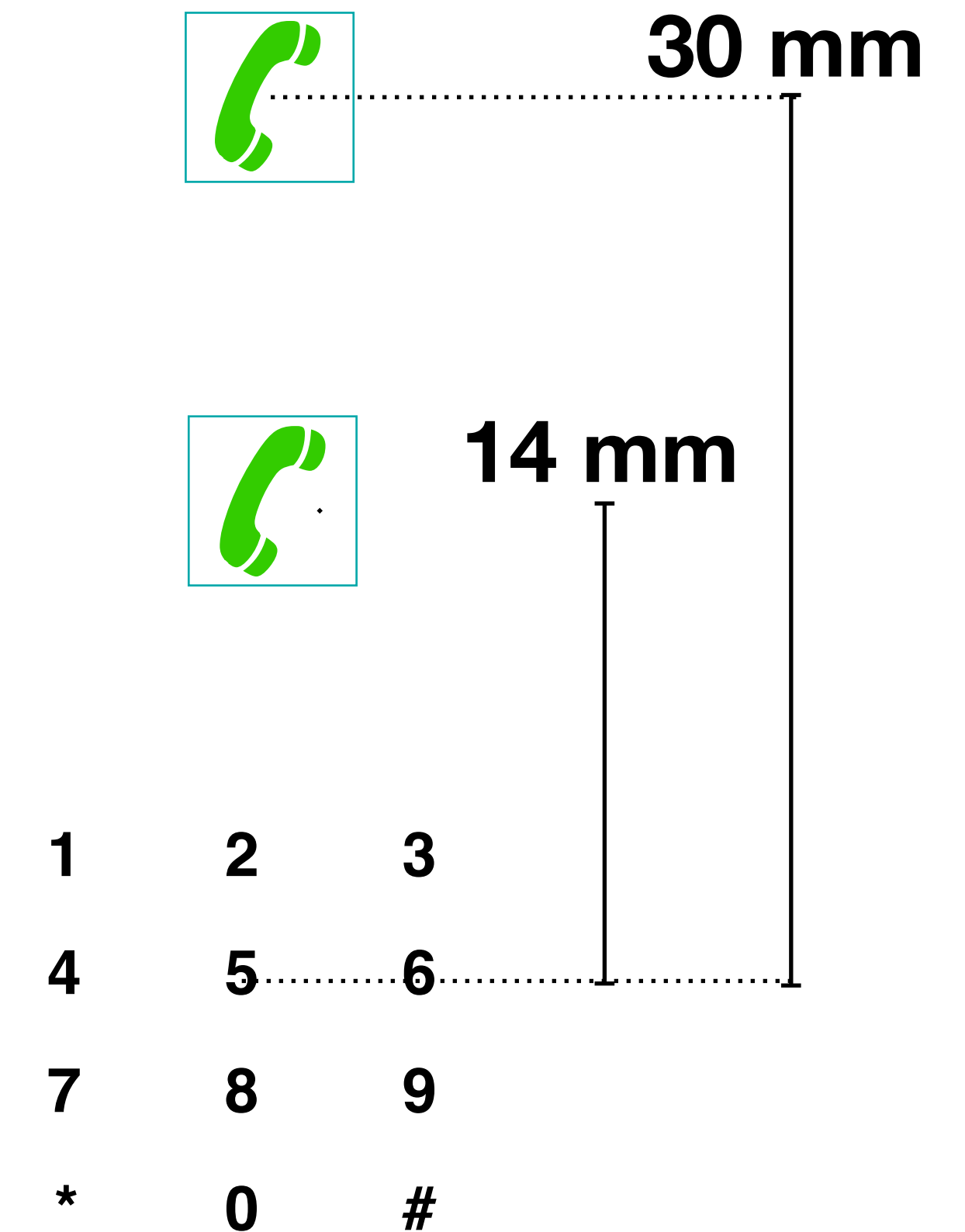




# In-Class Exercise: Mobile Phone



- How much faster does calling become by moving the “call” button from 30 mm distance to 14 mm distance, measured from the middle of the keypad? The size of the call button is 2 x 2 mm
- Shannon’s Formulation:  $T_{pos} = a + b \cdot \log_2\left(\frac{D}{W} + 1\right)$
- Use  $a = 0$  ms,  $b = 100$  ms/bit



# Solution

$$T_{pos1} = a + b \cdot \log_2\left(\frac{D_1}{W} + 1\right) \quad T_{pos2} = a + b \cdot \log_2\left(\frac{D_2}{W} + 1\right)$$

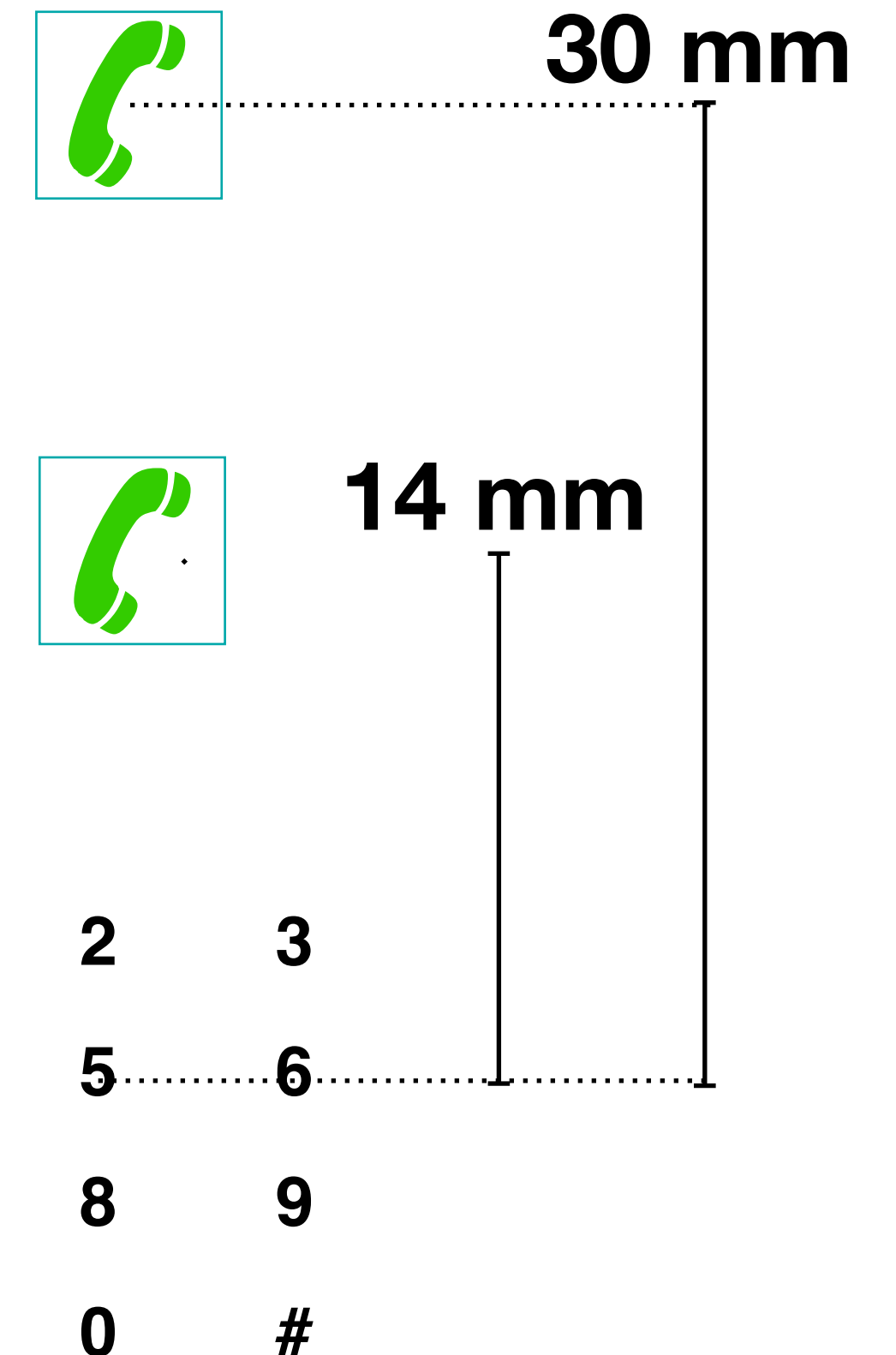
$$T_{Diff} = T_{pos1} - T_{pos2} = a + b \cdot \log_2\left(\frac{D_1}{W} + 1\right) - (a + b \cdot \log_2\left(\frac{D_2}{W} + 1\right))$$

$$= b \cdot (\log_2\left(\frac{D_1}{W} + 1\right) - \log_2\left(\frac{D_2}{W} + 1\right))$$

$$= b \cdot (\log_2\left(\frac{30}{2} + 1\right) - \log_2\left(\frac{14}{2} + 1\right)) = b \cdot (\log_2(16) - \log_2(8))$$

$$= b \cdot (4bit - 3bit) = b \cdot 1bit = 100 \frac{ms}{bit} \cdot 1bit = 100ms$$

⇒ Moving the call button speeds up each call by an average of about 100ms.





# Summary

- The Media Computing Group does cool stuff
- HCI is about humans, computers, the design process, and the social context
- The CMN model allows estimating reaction times and memory performance
- You can calculate the average movement time of pointing devices using Fitts' Law
- You've experienced that mathematical laws seem to govern your perception, memory, and movement

# What to Do Now

## Today

1. Register for the course on RWTHonline
2. Upload your signed Declaration of Compliance on our website  
(If you have done this already, you don't need to upload it again)

**File Name:** DIS1\_DoC\_<your last name>\_<matriculation number>.pdf

## Before next Lab on Tuesday

- Buy Don Norman's The Design of Everyday Things (2nd edition, 2013)